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ABSTRACT

There is a strong Air Force need for actuators capable of simultaneous large forces and strains in the form of complex three-dimensionally distributed actuation motions. A new active material knitted architecture generates complex three-dimensional distributed motions with simultaneous large force and strain within a compact package. The goal of this research was to establish a model-based foundation for exploration of this promising new actuation approach. Three research tasks were completed. The first task developed an active knit architectural hierarchy identifying the actuation mechanisms and correlating motions to hierarchical levels, enabling exploration of the full breadth of possible actuation motions. The second task derived a two dimensional analytical model, providing a tractable tool for prediction, design, and tailoring of planar contractile active knits. The third task demonstrated a flow control case study which evaluated the applicability of active knits and investigated their ability to create the desired kinematic actuation motions under the aerodynamic loads required for flow control. This research provides the fundamental knowledge of active knits required to further develop them as an enabling technology for a new generation of Air Force applications with novel functionality, expanding operational platform for greater mission adaptability.

EXECUTIVE SUMMARY

There is a growing need for actuators capable of concurrent radical forces and strains that produce three-dimensionally complex motions, distributed throughout a structure in a small package size. This need is particularly evident in the aerospace sector, which has an interest in configurable multifunctional structures that have the ability to dramatically alter their shape, functionality or mechanical properties in response to environmental or operational conditions to improve aircraft efficiency [1]-[2]. Substantial research has been conducted on actuator technologies to advance the current state of the art; however, the desired distributed complex motions with large simultaneous forces and strains have remained elusive. One actuation architecture that shows great promise is the active knit architecture, an internally leveraged network of unit cells that enables complex actuation motions with scalable radical kinetic performance. The goal of this research was to develop the fundamental scientific understanding of the active knit actuation architecture to enable the analysis and synthesis of simultaneous large force and strain actuators that produce complex three-dimensionally distributed actuation motions in a compact package.

ACTIVE KNIT HIERARCHICAL ARCHITECTURE

An active knit hierarchy (as detailed in section 2) was developed to establish a formal language and a hierarchical classification structure that identifies the actuation mechanism and links the kinematic actuation motion to the hierarchical level. The hierarchy enables exploration of the full breadth of possible actuator motions and provides a foundation for the modeling effort, an understanding for design, and insight into feasibility for applications. To capture the breath of kinematic actuation motions produced by active knits, the knitted hierarchy requires four levels that capture 1) multiple types of unit cells, 2) homogeneous distribution of unit cells across the knitting grid of the textile, 3) heterogeneous distribution of unit cells across the knitting grid of the textile, and 4) non planar orthogonal knitting grids. To capture these complexities, a four level active knit hierarchy (knitted loop, knit pattern, grid pattern, and restructured grid) was developed. The knitted loop leverages bending in the smart material to create larger actuation motions. The knit pattern, a homogeneous arrangement of knit and purl loops in the knitting grid, transforms the individual motions of the knitted loops into distributed actuation behaviors. heterogeneous patterns of knit and purl loops, produce different motions over different regions of the textile. Restructured grids, modified orthogonal knitting grids, transform and expand the type of motions produced at the lower levels of the hierarchy. The active knit hierarchy provides a classification scheme and illustrates numerous representative active knits to provide a useful catalog of a variety of complex motion capabilities that delivers insight that aids in the understanding, modeling, and design of this new actuation paradigm to meet growing actuation needs.

TWO-DIMENSIONAL ANALYTICAL MODEL OF PLANAR ACTIVE KNITTED LOOPS

A two-dimensional analytical model was developed (as detailed in section 3) to provide predictive capabilities for the fundamental knitted loops (knit and purl) that captures the kinematic and kinetic performance of the knitted loop and two-dimensional knit patterns and provides a tractable tool for prediction, design, and tailoring of planar contractile active knits. An analytical state-based actuation model was derived for the planar knitted loop in the garter knit pattern fabricated from variable stiffness smart material wire which accounts for the loading path and the friction between interlacing adjacent loops. The states of operation were defined based on the mechanical loading of the textile, the transition between different material stiffness, and the paths followed to arrive at each state. Operational transitions between these states induce frictional

forces (stick or slip) depending upon the state and path, which affect the actuation response. An analytical model was derived using Elastica Theory and Euler-Bernoulli beam bending and experimentally validated, providing predictive capabilities for the net actuation motion as a function of the applied tensile load on the textile. The model was validated experimentally for an SMA garter knit textile over a range of applied forces with good correlation (4.1% - 6.1% average relative displacement error for each extended state, 2.8% average relative displacement error for the contracted state, and 2.0 mm absolute displacement error for the actuation). The two dimensional analytical active knit loop model provides the ability to predict actuation motions for the large stroke, large force garter knit pattern actuation architecture (250% recoverable strain and over 50% actuation), enabling the design of planar contractile active knitted architectures for a wide range of applications and providing the foundation for models of more complex knitted architectures that produce three-dimensional actuation motions.

FEASIBILITY DEMONSTRATION – FLOW CONTROL CASE STUDY

A flow control case study (as detailed in section 4) was conducted to evaluate the applicability of active knits through an application case study that investigates the ability of active knits to create the desired kinematic actuation motions under application-level kinematic loads while addressing application implementation issues. This feasibility demonstration study was conducted using rib knit pattern active knits to meet the performance specifications required to change the shape of an aircraft wing to provide flow control. Rib knit pattern active knits actuate normal to the surface, producing span-wise discrete periodic arrays that can withstand aerodynamic forces while supplying the necessary displacement for flow control. The technical specifications for the contour bump applications were identified from existing theoretical research. The orientation and configuration of rib knit pattern textiles were selected such that the active knit actuator can withstand aerodynamic pressures while supplying the necessary displacement for flow control. Two rib knit pattern active knit prototypes were created and tested using a specially designed experimental rig (producing 6.3 and 6.4 mm actuation displacement under 2.5 and 1.4 kPa). Series and parallel combinations of identical rib knit pattern prototypes were experimentally explored to meet the technical specification required by the contour bump application. The measured knit performance was on the scale of the necessary aerodynamic pressures and displacements (with three sets of two nestled prototypes simultaneously actuating 20.8 mm under a 11.1 kPa load); thus, the rib knit pattern active knit is promising as a technical solution for distributed actuation of local surface profiles in flow control. This feasibility demonstration study shows that active knit pattern textiles can be used in applications by exploiting their unique performances to meet the kinematic and kinetic specifications of new applications.

CONCLUSION

Active knits are a new cellular architectural paradigm with the potential to revolutionize actuators by producing simultaneous radical forces and displacements, in the form of complex three-dimensional actuation motions distributed throughout a structure, all in a small package size. This research provides the fundamental knowledge needed to develop active knits as an enabling technology to meet the demand for advanced actuators. The radical forces and strains and complex, distributed, three-dimensional behaviors of these architectures go well beyond anything currently accessible through traditional actuation or conventional smart material actuation architectures. While active knits provide significant promise, more research is needed to fully develop this actuation architecture. With future research, this novel technology holds promise to enable advancements in current applications (shape morphing, flow control, deployable structures, etc), as well as open the door to applications yet conceived.

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1. Introduction

Actuators move our world. While actuators have enabled myriad technologies, there are still countless applications that are limited by available actuation approaches. For example, there is a strong need in several application fields for simultaneous large force and displacement actuators that create complex, three-dimensional actuation motions distributed through a structure in a small package size. While conventional and smart material based technologies cannot fulfill this need, new cellular smart material architectures show great promise. The goal of this research is to develop the fundamental scientific understanding of the active knit actuation architecture, which has shown the potential to deliver simultaneous radical forces and strains in variety of complex, distributed actuation motions.

1.1. GROWING ACTUATION NEED

There is a growing need for actuators capable of concurrent radical forces and strains that produce three-dimensionally complex motions, distributed throughout a structure in a small package size. This need is particularly evident in the aerospace sector, which has an interest in configurable multifunctional structures that have the ability to dramatically alter their shape, functionality or mechanical properties in response to environmental or operational conditions to improve aircraft efficiency [1]-[2]. One such multifunctional structure is morphing aircraft that can adjust their wing geometry to expand the aircrafts' operational platform and allow it to efficiently maneuver over a large range of flight regimes [3]. Another application, active flow control, requires the implementation of a multifunctional structure to create a controlled and varied texture across a surface to delay or reattach a separated boundary layer in order to reduce surface drag and improve flight efficiency [4]-[8]. Additionally, deployable space structures such as stabilization booms, solar arrays, communication reflectors, and telescopes need to be compactly stowed in launch vehicles then undergo radical deformations to recover the large structures in space [9]-[14].

Other areas such as the medical device and automotive fields would also greatly benefit from actuator advancements. For example, the medical field needs actuators that can produce large distributed strains that can be used in or on the human body to realize technologies that diagnosis, repair, and rehabilitate, such as field bandages and contracture tissue expanders that contract of expand over a large surface area [15], guided catheters that can navigate the complex curved conduits of the body [16], and implantable devices that can provide large mechanotransductive strains [17]. Similar needs arise in the automotive field to advance technologies that improve vehicle efficiency and customer satisfaction such as active air dams [18] and louvers [19] that provide flow control over the surface of the vehicle body and through the engine, morphing bumpers [19] that reshape areas of the body after an accident, and seat belts [20] that supply distributed restraint during rapid deceleration. These diverse applications illustrate a common need for actuators capable of simultaneous large forces and strains in the form of complex three-dimensionally distributed actuation motions.

1.2. CURRENT ACTUATOR STATE OF THE ART

Myriad applications (including medical devices, automotive, deployable structures, and aircraft) require advanced actuators that are capable of concurrent radical forces and strains while creating complex multi-dimensional actuation motions that are distributed throughout a

structure. Substantial research on actuator technologies has been conducted; however, these actuator characteristics have remained elusive.

1.2.1. Conventional Actuators

The proliferation of conventional actuators (electromagnetic, hydraulics, and pneumatics) has enabled countless applications. However, as demand for new applications increases a different genre of actuators are required to meet the application needs. There is a growing need for actuators capable of producing large three-dimensionally complex distributed actuation motions in a small package. Conventional actuators are established technologies that are capable of balancing force, stroke, and speed. However, they have difficulties providing more than point actuation. Because conventional actuators are typically point actuators they are not capable of producing distributed actuation motions or complex out-of-plane motions without incorporating additional mechanism. Even if conventional actuators could create the desired motions, they do not to meet the packaging requirement, which requires a high energy density. Most conventional actuators have energy densities orders of magnitude less than smart materials [21]. One exception is hydraulic actuators, which have similar energy density to that of Shape Memory Alloys (SMAs). While hydraulic actuators are energy dense, they have complex supporting infrastructure such as pumps and hydraulic lines that are large and difficult to package, making the system less than optimal.

1.2.2. Smart Material Actuators

Smart materials (materials that have the ability to transform energy from one domain to another) are energy dense actuators that have long held the promise of increasing the actuation authority and decreasing weight/size by an order of magnitude because of their high energy/power densities [21] (up to two or three orders of magnitude for Shape Memory Alloys vs. electromagnetic actuators). Unlike conventional actuators, smart materials are inherently distributed as they undergo deformation throughout their entire volume. While smart materials show promise for creating distributed actuation in a small package they still struggle to create simultaneous large strains and large forces. Unfortunately, smart materials that have large strains (greater than 100%), such as electroactive polymers and piezopolymers, have very low forces (in the milliNewton range) [22]-[25]. Alternatively, materials capable of modest force generation typically suffer small strains: 0.1-0.2% for piezoceramics, 1-2% for single crystals, 4-8% for shape memory alloys (SMA), and 3-5% for ferromagnetic SMAs [26]-[31]. Additionally, smart materials on their own are not capable of creating complex three dimensional motions.

1.2.3. Smart Material Actuator Architectures

While bulk smart materials cannot meet the growing actuation needs, they can be exploited in smart material actuator architectures to produce actuators capable of concurrent radical forces and strokes in the form of complex multi-dimensional actuation motions distributed throughout a structure. A smart material actuator architecture is the configuration of a raw form of a smart material into an actuator form that amplifies the force, displacement, and/or the type of motion produced by the base smart material. There are four types of smart material actuator architectures that have been employed to improve kinetic or kinematic actuation performance – frequency leveraged actuators, combinatorial actuators, externally leveraged actuators, and internally leveraged actuators. Each of these actuator architectures enhance the capabilities of

the base smart material by improving kinetic performance (either through enhanced force or displacement) and/or providing complex three dimensional motions.

1.2.3.1. Frequency Leveraged Actuation Architectures

Frequency leveraged actuators are smart material actuation architectures that accumulate a sequence of small deformations to produce larger actuation displacements. Numerous frequency leveraged architectures have been developed to enhance the displacements provided by the base smart material. For example, SMA ratchets combine a series of small ratchet steps to produce large linear actuation displacements, enabling applications such as implantable medical devices [17]. Piezoelectric inchworms use multiple individual actuators to clamp and progress a shaft through the actuator architecture [32], the individual steps enables the actuator to produce large precise motions such as those needed for optics alignment and precision machining. A final example are piezoelectric ultrasonic actuators, which actuate the piezoelectric actuator at one of its resonant frequencies to create an acoustic wave that propagates the moving part along a smooth, low friction contact surface [33]. While ultrasonic actuators can be used for numerous large displacement high precision applications, their true strength is their enhanced energy density when compared to electromagnetic motors [34]. Frequency leveraged actuation architectures provide simultaneous large forces and displacements by enhancing actuator displacement but they are limited because they do not produce complex distributed motions.

1.2.3.2. Combinatorial (Building Block) Actuation Architectures

Combinatorial actuation architectures are building block actuators that enhance the force and/or displacement of smart material actuation architectures by combining individual actuators in series and/or parallel. The series and parallel assembly of leveraged architectures produce actuators with enhanced kinetic (force displacement) performance by using the individual elements as building blocks or unit cells. For example, piezoelectric [35] and dielectric elastomer stacks [36] use individual pieces of material in series to produce enhanced displacements under the same applied load. Alternatively, bundles of SMA wires (parallel SMA wires) [37] have been used to enhance force output. Additionally, some leveraged actuation architectures (such as the piezoelectric Recurve [38] or C-block [39]) can be used as building blocks to improve force and displacement output over that of individual actuators. Combinatorial actuators are the most simplistic actuators that follow scaling rules for kinetic performance. While combinatorial actuators are a great, streamlined way to enhance the distributed force and displacement of actuators, they are limited in their ability to create three-dimensional complex motions.

1.2.3.3. Externally Leveraged Actuation Architectures

Externally leveraged actuation architectures connect the base smart material to external leveraging structures or mechanisms that transform the material output to produce a tailored performance to meet application needs. There are numerous types of externally leveraged actuators. Many externally leveraged architectures enhance the stroke provided by large force actuators (such as piezoelectric or magnetostrictive), or enhance the force output of large strain smart material actuators (such as EAPs). Other externally leveraged actuators are used as transducers that transfer lateral material displacements into actuator displacements in the normal direction. For example, piezoelectric Moonies [40], Cymbals [41], and X-frames [42], dielectric elastomer spiders [43], and smart material levers all provide actuation motions normal to the

material actuation direction. Frequently, the material leveraging that improves the actuation motion is done so at the cost of actuator force output. Externally leveraged architectures can also be used to create shaped, distributed planar actuation. Dielectric elastomer bowties [43] and flexible frames [43] employ an external frame to pre-stress the base smart material and create uniquely shaped actuators; however, they provide small actuation loads. To create even more complex motions, smart material actuated compliant mechanisms [44]-[47] have been employed. While compliant mechanisms have been used to change the shape of a wing [44]-[47], the output motion created by compliant mechanisms is distributed across a surface rather than throughout a structure. All of these externally leveraged actuation architectures use a smart material to supply the actuation motion while an external structure or mechanism produces the desired shape change. This increases the amount of non-actuating material in the structure and increases the overall size of the actuator, therefore reducing the energy density of the actuator. While externally leveraged actuation architectures are approaching complex motion, they are not able to provide simultaneous forces and displacements, and if they do, the motions are not complex.

1.2.3.4. Internally Leveraged Actuation Architectures

Internally leveraged actuators use the internal stress in the structure to leverage the base smart material to provide enhanced actuation motions in an energy dense package. There are numerous types of internally leveraged architectures that vary in complexity. simplistic are the internally leveraged geometries (such as SMA coil springs [48], SMA leaf springs [49], SMA torsion tubes [50], and EAP spring rolls [51]) that use the base smart material in a more complex state of stress (bending, torsion) to deliver a small set of basic actuation motions such as extension, bending, and torsion that are distributed throughout the actuator, but they do so with a sacrifice to the force of the actuator. A subsection of internally leveraged actuation architectures are induced strain actuators, which are composite actuators with multiple active elements or active elements mixed with passive elements that leverage the internal stresses of the smart material to create bending and torsional actuation motions. Various smart materials have been used to create active composites in the form of laminates [52][53], fibers [54]-[56], and particulates [57]. The motion output of the composite depends on the construction of the composite and the stress field of the material and can produce extension, bending, torsion, and combined motions. While active composites can generate mildly complex bending and twisting motions, the motions are not of the order desired for new applications and many composites suffer from debonding [54]. More sophisticated smart material composites, such as functionally graded piezoceramics [58], have led to the development more reliable composite structures and have the potential to create complex distributed motions, although not yet realized. Another type of internally leveraged actuation architectures is cellular actuators that use one (or more) unit cells of an internally leveraged smart material architecture by combining the unit cells in series and parallel to create two or three-dimensional structures; however research on cellular architectures has been limited. Smart material foams, such as shape memory polymer foam [59], have particulate inclusions and are promising for self-healing structures, but the material distribution could be optimized to achieve desired mechanical properties or obtain a predetermined shape upon actuation. Another promising cellular architecture is SMA Superelastic SMA honeycombs [60] have been experimentally tested with honeycombs. hexagonal and wavy-corrugated architectures that are capable of undergoing large, recoverable displacements under compressive loadings. Internally leveraged cellular architectures are extremely promising because through combinations of unit cells, the kinematic and kinetic

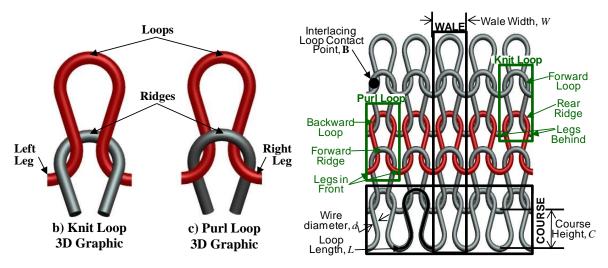


Figure 1. Active Knit Architecture. a) the active knit unit cell – knit and purl loops, b) the garter knit pattern architecture.

performance of the actuator can be controlled. Cellular architectures could provide the ability to tailor the performance; the individual unit cells can be used as building blocks to amplify the kinetic performance and adjacent unit cells can be manipulated in non-uniform distributions so that complex actuation motions can be designed and achieved. Cellular actuation architectures are an extremely promising approach that may have the ability to advance the capabilities of actuators and progress applications.

1.3. ACTIVE KNITS

Active knits are a novel type of internally leveraged cellular architecture that shows great promise. The internally leveraged network of unit cells that compose the active knit architecture enables complex distributed actuation motions with scalable radical kinetic performance. Active knits are capable of generating large strains beyond the base material because of their unique architecture and operation.

1.3.1. Active Knits Architecture

Active knits are a smart material fiber based actuation architecture that provides complex three-dimensional distributed actuation motions with enhanced kinetic performance through a hierarchically organized cellular network of interlacing adjacent loops of a single strand or fiber. Knitted textiles (traditional and active) have a hierarchical architecture that is based on a knitting grid of unit cells combined in orthogonal rows (courses) and columns (wales). The knit architecture is differentiated from other textile architectures (weaving, braiding, stitching, etc) by its unique unit cells – the knit and purl loops (Figure 1a). These unit cells are composed of a 180° bulb-shaped loop extending into two legs that interlock with a ridge formed by the previous row. The loops are distinguished by the position of the ridge (rear ridge for knit loop, forward ridge for purl loop). The knitted loops are geometrically defined by their course height (C), wale width (W), loop length (L), and fiber diameter (d). The course height (C) is the vertical distance between identical reference points of adjacent rows. The wale width (W) is the horizontal distance between identical reference points on adjacent loops within a course. The loop length (L) is the length along the centerline of the fiber of a single knit loop. The fiber diameter (d) is the diameter of the foundational wire.

The knitted loop unit cells can be combined to provide a wide variety of knit pattern textiles, which are defined by the arrangement of knit and purl loops. The most basic knit pattern, garter, has a symmetric arrangement of alternating rows of knit and purl loops (Figure 1). A course is a row of knitted loops, shown in red in Figure 1, which is composed of a single strand of alternating (up and down) curved loops. A wale is a column of knitted loops, the legs of each loop interlock with the top of the next loop down the wale (i.e. in the next course). In a course of knit loops, the legs of the upper loop in a wale overlap the top of the lower loop in the same wale and interlace behind the sides of the loop. Whereas, in a course of purl loops, the top of the lower loop overlaps the legs of the upper loop, which interlace behind the sides of the lower loop. The garter knit pattern, which is composed of alternating courses of all knit and all purl loops, forms a planar textile symmetric about the front and back. Numerous knit patterns can be created by changing the distribution of the knit and purl loops across the wales and courses of the textile. Regardless of the knit pattern, the loops within the architecture provide large curvatures through which loops interlace with the adjacent loop making contact at the interlacing contact point, **B**. The interlacing contact point is not a static point – it may change position as adjacent loops slip relative to each other during actuation.

1.3.2. Active Knits Operation

The operation of active knits is an important component of creating the large complex actuation motions. Active knits go through operational transitions from one state to another resulting in a change in length, shape, and stiffness of the textile. In the case of SMA active knits the operational transitions are initiated by either a change in thermal loading, inducing a material transition from flexible Martensite to stiff Austenite (called the Shape Memory Effect), or by changes in mechanical loading. Typically, upon actuation the smart material fiber tries to return to its original, stress-free straight shape by recovering the strain induced in the smart material fiber during loop formation. The resulting actuation motion depends on the architecture of the active knit textile.

For symmetric garter knit pattern active knits, the fiber straightening causes the height of the individual loops to decrease (while slightly expanding the width) and the loops may slip relative to each other in the plane in which they lie. The change in loop geometry reduces the total length of the active knit textile which results in textiles with net strains that are orders of magnitude higher than the local strains within the material itself. The general actuation motion is harnessed in a four step (Figure 2) actuation process.

1.3.2.1. Step 1: Austenite Free State

A typical garter knit pattern actuation cycle is initiated with the SMA textile in a heated state (Austenite) with no external loads (Free). The increased temperature causes the material to transition from the soft martensite phase to the stiff austenite phase. When heated the loops attempt to return to their naturally straight configuration resulting in a relatively wide wale width, W, and a relatively short course height, C. Even though many internal stresses and strains exist, the garter knit textile in the Austenite Free State (Figure 2 a) is set as the zero deflection reference point for actuation.

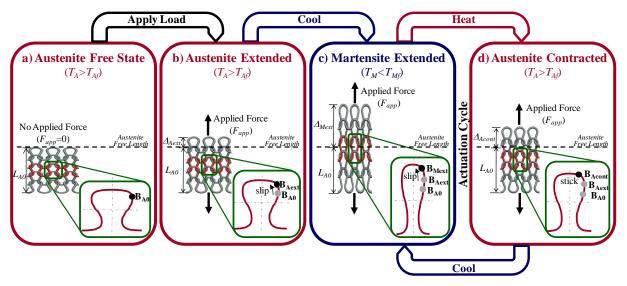


Figure 2. Active Knit Operation. a) Austenite Free State, b) Austenite Extended State, c) Martensite Extended State, and d) Austenite Contracted State reached through thermal or mechanical operational transitions where a typical actuation cycle is alternates between the Martensite Extended and Austenite Contracted States.

1.3.2.2. Step 2: Austenite Extended State

When a tensile load is applied to the textile in this heated state, the knit loops elongate, increasing the course height, C, and lengthening the entire textile into the Austenite Extended State (Figure 2b).

1.3.2.3. Step 3: Martensite Extended State

When the textile is allowed to cool under load to a temperature below its martensite finish transition temperature, the textile makes a material transition into the martensite phase and becomes less stiff. As a result, the course height of the loops elongates further into the Martensite Extended State (Figure 2c). The Martensite Extended State is the first of two states in the cyclic portion of the typical actuation cycle.

1.3.2.4. Step 4: Austenite Contracted State

The next state of the actuation cycle is entered when the material is heated under load to above its austenite finish transition temperature to the austenite phase. The resulting stiffening of the material causes the fibers within each loop to attempt to straighten to their natural straight shape, reducing the course height, and inducing contraction of the textile into the Austenite Contracted State (Figure 2 d).

The hierarchical knit architecture transforms the contractile actuation strains of SMA fiber into very large three dimensional motions because individual loops change shape (height, width, and curvature) and propagate this amplification through the textile. The hierarchical architecture of active knits leverages the bulk material behavior to provide complex three-dimensional actuation motions distributed across a surface or throughout a structure.

1.3.3. Research Issues

Active knits show tremendous potential as an actuator technology, but they are in their infancy and no science base has been established to design, synthesize, and analyze this architecture. To realize and evaluate the potential of this new architectural framework three research areas need to be developed: active knit hierarchical architecture classification, active knit modeling, and case studies.

1.3.3.1. Hierarchical Architecture Classification

To effectively use the active knit technology in applications a formal language that describes the active knitted architecture needs to be constructed. Additionally, a hierarchical architecture classification structure is essential to identifying the actuation mechanism and determining the impact of architecture on kinematic actuator performance. In order for the active knit hierarchy to reveal the breadth of kinematic actuation motions produced by active knits, the knitted hierarchy must describe four component levels: 1) multiple types of unit cells, 2) homogeneous distribution of unit cells across the knitting grid of the textile, 3) heterogeneous distribution of unit cells across the knitting grid of the textile, and 4) non-planar orthogonal knitting grids. A complete understanding of the active knit hierarchy and a common language for discussion is needed to derive models and demonstrate feasibility to realize applications.

1.3.3.2. Active Knit Modeling

Models of the active knit structures must be developed to enable performance prediction and design synthesis. Because active knits are complicated hierarchical structures the modeling process should be simplified by identifying the smallest repetitive element – the unit cell. Because of the variety of knitted structures the knitted unit cell must be defined independently for each knit structure. To accurately model the behavior of the active knit it is essential that the model incorporates the dual state nature of the foundational wire, captures the large rotations of the wire in the formed knitted loop, and accounts for friction between interlacing adjacent loops. While executing the model it must transition between a set of defined states that account for the thermal and mechanical operational transitions that influence the load path and the interlacing loop friction that match the experimental conditions. The model must be built up to represent the entire knit structure by combining the unit cell model in series and parallel. It is necessary to develop models to provide design and analysis capabilities through model implementation.

1.3.3.3. Experimental Validation

A model must be experimentally validated to ensure the accuracy of its predictive capabilities. Because each of the active knit architectures display radically different kinematic actuation behaviors a different experimental setup and procedure is needed for each knit architecture. When designing the experiments it is necessary to ensure that each active knit architecture is tested for a particular motion and loading profile that is related to a potential application because a single type of experiment cannot capture and characterize the behavior of all active knits.

1.3.3.4. Case Studies

The need for case studies is two-fold: 1) to assess the models and design guidelines, and 2) to demonstrate the ability of active knits to meet the kinematic and kinetic actuation specifications of new applications. To conduct a case study it is first necessary to identify a

potential application, and then the kinematic motion and kinetic performance specifications of the application need to be identified and developed. An active knit architecture should be chosen for its ability to create the desired kinematic motion. Meeting the kinetic specifications of the application requires exercising the model and/or employing the design guidelines to determine the geometric parameters necessary to meet the simultaneous force and displacement requirements. The feasibility demonstration study should show that active knit pattern textiles can be used in applications by exploiting their unique performances to meet the kinematic and kinetic specifications new applications.

1.4. RESEARCH GOALS AND OBJECTIVES

The goal of this research was to develop the fundamental scientific understanding of the active knit actuation architecture to enable the analysis and synthesis of simultaneous large force and strain actuators that produce complex three-dimensionally distributed actuation motions in a compact package. Three research objectives were crucial to meeting this goal.

- 1. **Hierarchical Knit Architecture Classification.** Establish a formal language and a hierarchical classification structure that will identify the actuation mechanism and link the kinematic actuation motion to the hierarchical level, enabling exploration of the full breadth of possible actuator motions and providing a foundation for the modeling effort, an understanding for design, and insight into feasibility for applications.
- 2. **Fundamental Knitted Loop Modeling.** Develop predictive capabilities for the fundamental knitted loops (knit and purl) that will capture the kinematic and kinetic performance of the knitted loop and two-dimensional knit patterns by accounting for the dual state nature of active knits and friction between interlacing adjacent loops, providing a tractable tool for prediction, design, and tailoring of planar contractile active knits.
- 3. **Application Feasibility Demonstration.** Evaluate the applicability of active knits and their supporting models and design guidelines through a design case study that investigates the ability of active knits to create the desired kinematic actuation motions under application-level kinematic loads while addressing application implementation issues.

It is necessary to address all these objectives to realize active knits as an enabler to numerous applications that require distributed complex three-dimensional actuation motions.

1.5. APPROACH

This research was broken into three activities to address the three primary objectives. A hierarchical framework was established to understand the breadth of the architecture and to correlate the architecture to the kinematic motion output. A two-dimensional knitted loop and garter knit pattern model was developed to provide predictive capabilities of an exemplary active knit architecture. A case study was performed to insure that active knits could be useful for a real application that requires concurrent radical forces and strains in the form of complex three-dimensionally actuation motions distributed through a structure. All active knits created for this research were produced using Dynalloy's Flexinol® 70°C shape memory alloy wire.

1.5.1. Active Knit Hierarchy

Active knits are an exciting new actuation technology; however there is not an existing science base by which they can be evaluated. Before predictive models can be derived or application feasibility can be demonstrated, a formal language that describes the active knit architecture must be developed and the breadth of the hierarchy must be determined. Most research on traditional and engineering textiles use a two-level hierarchy to describe the mechanical response of the textile. The first level of the hierarchy is the knitted loop, which is combined in series and parallel to form the second level, the knit pattern. While this cellular hierarchical approach has proved useful for traditional engineering knits, it lacks the sophistication and hierarchical levels needed to capture architectural variations that produce the large, complex, three-dimensionally distributed actuation motions that lend particular promise to active knits. To capture to breath of kinematic actuation motions produced by active knits, the knitted hierarchy must be expanded to four levels that capture 1) multiple types of unit cells, 2) homogeneous distribution of unit cells across the knitting grid of the textile, 3) heterogeneous distribution of unit cells across the knitting grid of the textile, and 4) non planar orthogonal knitting grids. To capture these complexities, a four level active knit hierarchy (knitted loop, knit pattern, grid pattern, and restructured grid) was developed. Each level of the hierarchy was defined and various architectural examples of each level of the hierarchy were experimentally tested for their kinematic performance.

- 1. **Knitted Loop:** The knitted loop is the first level of the hierarchy, which, as the fundamental unit that makes up a single cell in the knitted grid, leverages bending in the smart material to create larger actuation motions. There are two knitted loops in the knit architecture knit and purl loops. The knitted loops do not exist independently and must be constrained within a knit pattern, grid pattern, or restructured grid to display the large strain actuation behavior.
- 2. **Knit Patterns:** The second level, the knit pattern, is defined by the homogeneous arrangement of the interlacing knit and purl loops within the knitting grid of orthogonal rows and columns. The most basic knit pattern architecture is a knitting grid composed of a single type of loop (either all knit or all purl) called stockinette, which transforms from planar to scrolling upon actuation. Many other knit patterns are formed by combining both types of loops in striped patterns in the knitting grid: vertical stripes form rib knit patterns that create accordion-like motion upon actuation, horizontal stripes form garter knit patterns that provide planar contraction, and diagonal combinations form the seed knit patter that generates arches. Combining knitted loops across the knitting grid in different knit patterns transforms the individual motions of the knitted loops into distributed actuation behaviors.
- 3. **Grid Patterns:** The third level of the knit hierarchy, grid patterns, is composed of regions of knit patterns that are arranged spatially across the knitting grid to form more complicated, heterogeneous patterns. By varying the knit patterns used across the knitting grid, different motions can be produced over different regions of the textile. The most basic grid pattern is formed by synthesizing two knit loop patterns across a single textile. Combining knit loop patterns in a knit loop pattern distribution is a powerful tool that produces textiles that create controllable complex three-dimensional motions distributed heterogeneously over an entire surface forming variable surface actuators.
- 4. **Restructured Grids:** The fourth level, restructured grids, modifies the orthogonal knitting grid to provide textiles with restructured grids that transform and expand the type

of motions produced at the lower levels of the hierarchy. Four ways of restructuring the grid – Post-Knitting Connections, Course-Wise Restructuring, Grid Cell Merging, and Re-Ordered Grids – were investigated. Post-knitting connections provide a structure that can further leverage the underlying behavior of the knit pattern or grid pattern used in the construction of the textile. Course-wise restructured grids produce three-dimensional textiles that are constrained by the helically connected knitted loops, and produce novel out-of-plane motions a result of the skewed, asymmetric knitted loops of the restructured grid. Grid cell merging controls the boundary conditions though manipulation of the shape of the actuator, achieving new complex three dimensional motions and realizing alternative complex actuator shapes. Reordered grids create a restructured grid that produces tailorable motions that are not available from the basic knit loop patterns alone.

This classification and illustration of representative active knits provides a useful catalog of a variety of complex motion capabilities and delivers insight that aids in the understanding, modeling, and design of this new actuation paradigm to meet growing actuation needs. The complete details of the active knit hierarchy are provided in section 2 of this document.

1.5.2. Knitted Loop Model

To advance active knit technology and establish the science base to implement the technology in applications, a model that captures the kinetic performance of active knitted textiles is needed. Active knits are complicated hierarchical structures; therefore, the first step in creating a predictive model was to model the kinetic behavior of the first level of the active knit hierarchy – the knitted loop. Knitted loops are assembled according to the knitting grid to create knit patterns; therefore, the kinetic performance of the individual loops is scaled in series and parallel to predict the performance of knit pattern active knit textiles. While existing passive knit models serve as a foundation for the kinetic modeling of active knits no existing models are capable of predicting the actuation performance of active knits. However, existing models can be modified and combined to capture the actuation behavior of active knits by including the thermal and mechanical operational transitions that occur during active knit actuation and by including the influence of the load path and the interlacing loop friction. An analytical statebased actuation model of the planar knitted loop in the garter knit pattern fabricated from variable stiffness smart material wire which accounts for the loading path and the friction between interlacing adjacent loops was developed. The states of operation were defined based on the mechanical loading of the textile, the transition between different material stiffness, and the paths followed to arrive at each state. Operational transitions between these states induce frictional forces (stick or slip) depending upon the state and path, which affect the actuation response. A load-extension model was derived for each state of a typical actuation cycle with respect to the unit cell of a single loop of the textile based on the stress-strain behavior of the active material with assumptions made to allow analytical tractability. Elastica Theory and Euler-Bernoulli beam bending were used to capture the large deformations within a loop of wire. The resulting kinematic and kinetic relations for a single cell scaled the load-extension behavior of the entire knit textile for each state, and provided analytical algebraic transcendental expressions for the net actuation motion as a function of the applied tensile load on the textile. The model was validated experimentally for an SMA garter knit textile over a range of applied forces with good correlation (4.1% - 6.1% average relative displacement error for each extended state, 2.8% average relative displacement error for the contracted state, and 2.0 mm absolute displacement error for the actuation). The two dimensional analytical active knit loop model

provides the ability to predict actuation motions for the large stroke, large force garter knit pattern actuation architecture, enabling the design of planar contractile active knitted architectures for a wide range of applications and providing the foundation for models of more complex knitted architectures that produce three-dimensional actuation motions. The development and validation of the two-dimensional analytical model of the knitted loop and garter knit pattern are provided in detail in section 3 of this document.

1.5.3. Feasibility Design Study

Active knits are a promising actuation architecture that produces unique actuation motions which are unattainable with current technologies, however, the feasibility of using active knits in applications has yet to be demonstrated. A feasibility demonstration study was conducted using rib knit pattern active knits to meet the performance specifications required for flow control of an aircraft. Flow control has been of significant interest to the aerospace community because actively manipulating flow characteristics around the wing can enhance high-lift capability and reduce drag; thereby, increasing fuel economy and improving maneuverability and operation over diverse flight conditions which enables longer, more varied missions. Changing the shape of the wing to employ distributed actuators across the surface of the wing through the use of contour bumps is a theoretically promising way to control air flow over the wing; however, no actuators currently exist to achieve this task. Rib knit pattern active knits actuate normal to the surface, producing span-wise discrete periodic arrays that can withstand aerodynamic forces while supplying the necessary displacement for flow control. The technical specifications for the contour bump applications were developed from existing theoretical research. The orientation and configuration of rib knit pattern textiles were described such that the active knit actuator can with stand aerodynamic pressures while supplying the necessary displacement for flow control. Two rib knit pattern active knit prototypes were created and tested using a specially designed experimental rig (producing 6.3 and 6.4 mm actuation displacement under 2.5 and 1.4 kPa). Series and parallel combinations of identical rib knit pattern prototypes were experimentally explored to meet the technical specification required by the contour bump application. The measured knit performance was on the scale of the necessary aerodynamic pressures and displacements (with three sets of two nestled prototypes simultaneously actuating 20.8 mm under a 11.1 kPa load); thus, the rib knit pattern active knit is promising as a technical solution for distributed actuation of local surface profiles in flow control. This feasibility demonstration study shows that active knit pattern textiles can be used in applications by exploiting their unique performances to meet the kinematic and kinetic specifications new applications. The full flow control case study is described in section 4.

1.6. OUTCOMES AND CONTRIBUTIONS

Active knits are a new cellular architectural paradigm with the potential to revolutionize actuators by producing simultaneous radical forces and displacements, in the form of complex three-dimensional actuation motions distributed throughout a structure, all in a small package size. This research establishes a scientific basis for active knitted actuators. A newly developed language along with an active knit hierarchical classification describes the knitted architecture. A catalog of different active knit actuation motions and an understanding of the relationship between hierarchical level and kinematic actuation behavior provides insight that aids in designing active knit architectures capable of producing desired motions. Predictive capabilities are provided by analytical models of two-dimensional active knit architectures. A modeling

procedure is outlined that provides the foundation for other active knit architectures. Feasibility studies meeting the technical specifications for a flow control enabling actuator demonstrate the value of active knits as an enabling technology.

The contributions of this research extend beyond active knitted actuators, providing understanding of the bending within SMA and the behavior of general knitted textiles in elastic composites. The expanded knit hierarchy can be used to design complex architectures for traditional and engineering textile applications and the models can be used to enhance predictive capabilities. The improved handling of friction in the model can be used to predict hysteretic friction behavior, a capability not currently available. Additionally, the approach can be expanded to work with other active/passive material combinations and activation stimuli that may provide different performance characteristics (force, speed, frequency). Finally, the viability assessment for the case study application provides a useful guide for future development for any number of applications.

This research provides the fundamental knowledge needed to develop active knits to meet the demand for advanced actuators. The radical forces and strains and complex, distributed, three-dimensional behaviors of these architectures go well beyond anything currently accessible through traditional actuation or conventional smart material actuation architectures. This novel technology enables advancements in current applications (shape morphing, flow control, deployable structures, safety mechanisms, medical devices, etc.), as well as opening the door to applications yet conceived.

2. ACTIVE KNIT HIERARCHICAL ARCHITECTURE

Active knits are a new actuation paradigm. Because active knits are a new actuation technology, there is not an existing science base by which they can be evaluated. Before predictive models can be derived, or application feasibility can be demonstrated, a formal language that describes the active knit architecture must be developed. While traditional and engineering textiles do not undergo actuation, the mechanical response of these textiles has been investigated [61]-[86] and can provide some guidance for establishing the scientific foundation to investigate the mechanism and motion of active knit actuator architectures. Most research on both traditional and engineering textiles use a cellular approach to determine the behavior of textiles [82]-[86]. In these existing cellular methods, the textile is divided into a grid of unit cells that represent the smallest repeating element in a textile. The predicted performance of a single unit cell is extrapolated to represent the behavior of the entire textile. This two level hierarchical approach has been useful for identifying the extensional performance of plain knitted materials, which are those with the simplest knitted architectures. While this cellular hierarchical approach has proved useful for traditional engineering knits, it lacks the sophistication and hierarchical levels needed to capture architectural variations that produce the large, complex, threedimensionally distributed actuation motions that lend particular promise to active knits. To capture to breath of kinematic actuation motions produced by active knits, the knitted hierarchy must be expanded to four levels that capture 1) multiple types of unit cells, 2) homogeneous distribution of unit cells across the knitting grid of the textile, 3) heterogeneous distribution of unit cells across the knitting grid of the textile, and 4) non planar orthogonal knitting grids.

This section defines a hierarchical architectural classification for active knit actuators. This classification establishes language for clear communication of the variety of architectures. Additionally, the expanded classification structure unveils important behavioral trends of each hierarchical level and exposes lessons of how each level can be utilized to design knit actuators tailored to applications that need large, complex, three-dimensionally distributed motions. This classification provides a foundation for the modeling effort, an understanding for design, and insight into feasibility for applications.

Leveraging the cellular approach, the hierarchical classification of active knitted architectures (Figure 3) is based on a knitting grid with orthogonal rows (courses) and columns (wales). The architectural hierarchical classification extends the simple two-level hierarchy of traditional and engineering textiles to four levels

- 1. The first level of the hierarchy is the *knitted loop* which, as the fundamental unit within a single cell in the knitted grid, leverages bending in the smart material to create larger actuation motions.
- 2. The second level is composed of *knit patterns* in which the loops combine across the knitting grid in different ways, transforming the individual motions of the knitted loops into distributed actuation behaviors.
- 3. The third level, *grid patterns*, combines different regions of knit patterns over the knitting grid to produce complex, potentially non-homogeneous motions.
- 4. The fourth level, *restructured grids*, modifies the orthogonal knitting grid to provide textiles with restructured grids that modify and expand the type of motions produced at the lower levels of the hierarchy.

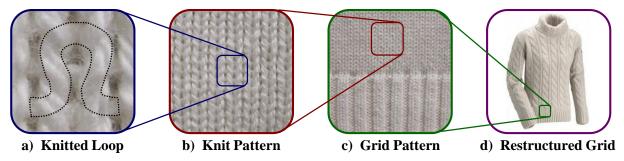


Figure 3. Hierarchical Knit Architecture. All knit materials are hierarchical structures where the behavior is influenced by each of the hierarchical levels a) Knitted Loops, b) Knit Patterns, c) Grid Patterns, and d) Restructured Grids.

In this section, each level of the hierarchy is defined and various architectural examples of each level of the hierarchy are provided. The active knit actuation mechanism is identified and the link between active knit kinematic behavior and hierarchical architecture level is described and experimentally examined. This classification and illustration of representative active knits provides a useful catalog of a variety of complex motion capabilities and delivers insight that aids in the understanding, modeling, and design of this new actuation paradigm to meet growing actuation needs.

2.1. LEVEL 1: KNITTED LOOPS

The first level of the hierarchical architecture is composed of two basic *knitted loops* – knit and purl (Figure 4) –which are the unit cells of the knit architecture. Both the knit and purl loops are unit cells made up of a loop, two legs, and a ridge. The loop is curved slightly more than 180°, creating a tear-drop shape that forms the upper portion of the knit unit cell. The loop extends into the legs, where adjacent unit cells attach to one another. The ridge is the uppermost portion of the loop from the previous course (row); the intersecting ridge divides the loop from the legs. The feature that distinguishes between the loops is the location of the loop and legs with respect to the ridge. The knit loop is created by passing through the loop in the previous course

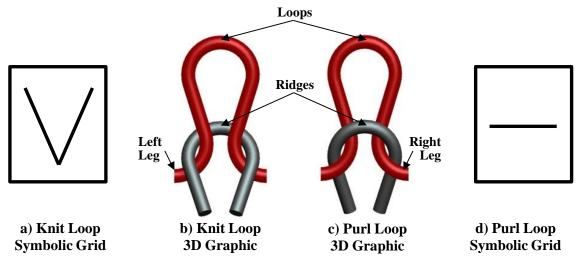


Figure 4. Knitted Loops. Two types of knitted loops make up the first level of the hierarchical knit architecture: a) the symbolic grid representation of a knit loop is a V, b) the 3D graphic of a knit loop shows a forward loop, rear ridge, and legs extending to the rear, c) the 3D graphic of a purl loop shows rear loop, forward ridge, and legs extending forward, and d) the symbolic grid representation of a purl loop is a horizontal dash.

from the back to the front and is characterized by a forward loop and a rear ridge. The legs of the knit loop interlock with the ridge, and then extend behind the ridge. Since the ridge is in the rear for knit loops only the base of the loop is visible; the base of the knit loop appears as a "V" like shape on the textile and is represented in the symbolic grid with a "V" (a standard notation in traditional knitting). The purl loop is the opposite of the knit loop. The purl loop is created by passing through the loop in the previous course from the front to the back and is characterized by a backward loop and a forward ridge. The legs of the purl loop interlock with the ridge, and then extend in front of the ridge. Because the ridge is in the front for purl loops it is visible; the ridge of the purl loop appears as a "-" like shape on the textile and is represented in the symbolic grid with a "-" (a standard notation in traditional knitting). A purl loop on one side of the textile appears as a knit loop on the other side.

Regardless of the fiber material, all knitted textiles demonstrate elasticity. This elasticity is a result of the curved loops, which allow bidirectional stretching as the loop is pulled height-wise or width-wise. The large curvatures induced during manufacturing result in large fiber strains. In the case of SMA wire, the wire, which is nominally straight, is bent into the loop shape when in the cold, relatively soft martensite state. When heated to the relatively stiff austenite state, the wire attempts to straighten, opening the loop, resulting in a reduced loop height and a slightly increased loop width. When allowed to cool, the wire returns to the martensite state and the loop relaxes. The bending and straightening of the base fiber occurs in both knit and purl loops within knitted textiles, however, the knitted loop alone does exist on its own and must be constrained in a knit pattern, grid pattern, or restructured grid to display this behavior. The unique loop structure of the knit architecture leverages the strain of the SMA wire, enabling the large distributed actuation strains of the active knit.

2.2. LEVEL 2: KNIT PATTERNS

The second level of the architectural hierarchy, the *knit pattern*, is defined by the homogeneous arrangement of the interlacing knit and purl loops within the knitting grid of orthogonal rows and columns. Knit patterns are nearly planar (i.e., they have a minimal out of plane thickness) textile swatches composed of multiple knitted (knit and/or purl) loops. The most basic knit pattern architecture is a knitting grid composed of a single type of loop (either all knit or all purl) called stockinette. Many other knit patterns are formed by combining both types of loops in striped patterns in the knitting grid: either vertical, horizontal, or diagonal combinations of knit and purl loops. The architecture of the knit pattern is composed of a homogeneous repeatable pattern and is defined by the type of knitted loops and location of adjacent knitted loops to one another within the knitting grid.

To investigate actuation behaviors of a variety of active knitted architectures at the knit pattern level, several prototypes of each knit pattern (stockinette, garter, welt, rib, and seed) were fabricated using traditional knitting needles and techniques with Dynalloy's Flexinol ® (SMA) wire with a transition temperature of 70°C. Wire diameters of 8 to 15 mil were knitted with needle diameters ranging from 3 mm to 10 mm (resulting in loop diameters of the same dimension). The knitted prototypes were heat-activated to full transition with a Heat Gun and their bulk behavior was observed.

2.2.1. Solid Knit Pattern – Stockinette

The solid knit pattern is created with a single type of knitted loop (Figure 5), either all knit

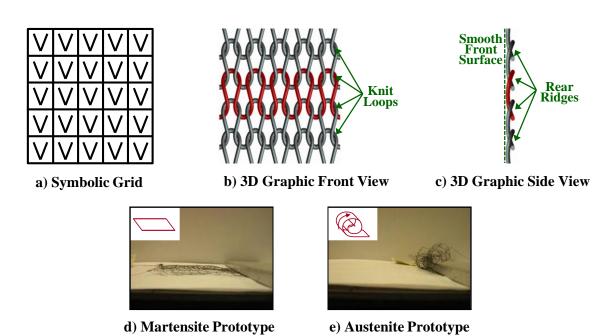


Figure 5. Solid Knit Pattern – **Stockinette.** The rolling actuation motion of stockinette is driven by the asymmetric architecture. Shown are the a) symbolic grid composed of all knit loops represented by V's, b) the front view 3D graphic of all knit loops, and c) the side view 3D graphic of the slight out-of-plane of curvatures that result in a smooth front surface and rear ridges. The pictures demonstrate the d) elongated prototype in cold martensite state and the e) rolled actuated prototype in the hot austenite state.

loops (represented by "V" in the symbolic grid) or all purls loops (represented by a "-" in the symbolic grid) appear in the knitting grid. There is only one type of solid knit pattern, stockinette, because a purl loop is the other side of a knit loop, and a solid pattern of purl loops is simply a solid pattern of knit loops flipped over. Therefore, either type of loop can be repeated to create the same knit loop pattern. The architecture of the stockinette forms an asymmetric topology about the front and back of the textile; the front side of the textile is smooth and resembles columns of "V"s from the knit loops, whereas the back side has rows of ridges from the purl loops. The asymmetric topology results from pulling each course of knitted loops from the back of the previous course to the front, causing the loops to arch out of the plane because each course lies on an offset cylindrical surface (Figure 5c). During thermal actuation, each course of loops attempts to straighten, forcing the shape of the loop to change because loops are constrained by adjacent loops. The height of the loop is reduced which forces the ridges toward one another, causing the loops to bend even further out-of-plane. This out-of-plane bending propagates through the textile resulting in a slight rotation between each course of knitted loops ending in a tube-like structure.

A prototype (Figure 5d, e) was constructed on 5.5 mm needles, using 8 mil wire and 10 loops to create a prototype 9 cm long. When heated above the transition temperature the prototype rolls into a tight scroll with an outer diameter of 2 cm, reducing the length of the textile by 80%. The solid knit pattern of stockinette creates a bending moment that creates a unique rolling motion which could enable applications such as complex deployable structures.

2.2.2. Horizontally Striped Patterns - Garter and Welt

Horizontally striped patterns are created when courses of knit loops are alternated with courses of purl loops in the knitting grid. When a single course of knit loops is alternated with a

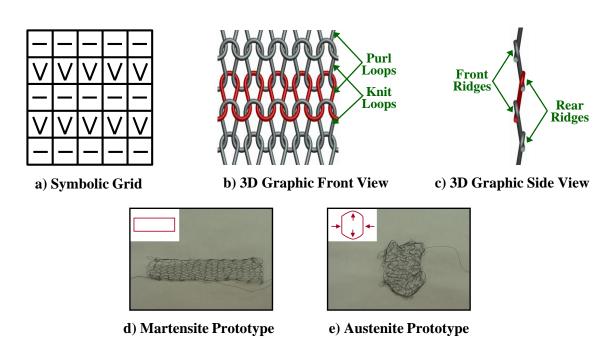


Figure 6. Horizontally Striped Knit Pattern – **Garter.** The distributed contraction of garter is driven by the symmetric architecture. Shown are the a) symbolic grid composed of alternating courses of knit (V) and purl (–) loops, b) the front view 3D graphic of alternating courses of knit and purl loops and c) the side view of alternating front and rear ridges. The pictures demonstrate d) the flat elongated prototype in the cold martensite state and e) the contracted prototype in the hot austenite state.

single course of purl loops, the horizontally striped knit loop pattern is called Garter (Figure 6). The architecture of the garter knit pattern results in a symmetric textile topology with consistent courses of horizontal ridges on each side of the textile. The alternating courses of knit and purl loops lie on angled planes (the loops are not bent as is the case for stockinette). The architecture of garter provides significant elasticity along the length of the textile. Because the type of knitted loop in each course is alternated in garter, adjacent courses lie flat in angled planes and the tops and bottoms of the loops form the symmetric ridges on either side of the textile. Upon thermal actuation of garter knit pattern active knits, the curved SMA fiber in each loop attempts to return to its original straight shape; causing the loops in each course to straighten and slip relative to each other in the plane in which they lie, reducing the total length of the textile.

To demonstrate the contractile behavior, a rectangular garter prototype (Figure 6d, e) was created with 15 mil wire on 5.5 mm diameter needles yielding a prototype with 10 loops in each course, for a total length of 20 cm. The prototype contracted in length by 73% while expanding horizontally 55%. The garter knit loop pattern leverages the motion produced by knitted loops, providing considerable strain amplification, an order of magnitude over material strain alone, and could be used as a distributed contractile surface actuator for applications requiring large motions with compact packaging such as morphing structures.

Another horizontally striped knit pattern – Welt – is created by alternating more than one course of knit loops with the same number of courses of purl loops (Figure 7) in the knitting grid. This produces a textile with alternating rows of smooth surfaces and rows of ridges (much like alternating a number of rows of stockinette front with stockinette back). The textile, which initially lies flat, actuates into a corrugated shape of alternating arched rows, increasing the thickness of the textile while decreasing the total length of the textile.

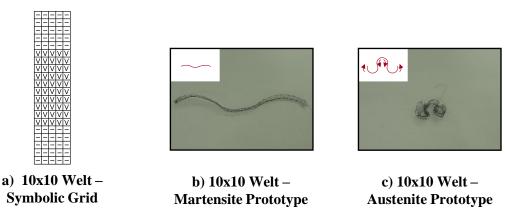


Figure 7. Horizontally Striped Knit Pattern – Welt. More complicated motions can be obtained by welt patterns, n courses of knit loops alternating with n courses of purl loops. Textiles knit following the a) 10x10 welt symbolic grid produces out-of-plane motion when the welt actuates from b) a flat elongated textile in the cold martensite state into c) a curled and contracted textile in the hot austenite state.

A 10x10 welt prototype (ten courses of knit alternating with ten courses of purl) was created using 8 mil wire, 5.5 mm knitting needles and 5 loops to demonstrate the welted behavior. The welt provided enhanced contractions (80%) over the garter knit pattern as the loops contractions were coupled with the out-of-plane bending. The horizontally striped knit loop pattern of welt textiles provides out-of-plane surface displacements that can be used to for surface texturizing actuators as well as extremely large contractile motions.

2.2.3. Vertically Striped Patterns – Rib

Vertically striped patterns (Rib – Figure 8) are created by alternating columns of knit loops with columns of purl loops in the knitting grid. This produces a textile with symmetric columns, alternating between smooth columns of the front of stockinette and columns of ridges of the back of stockinette. A 1x1 rib alternates a single column of knit loops with a single column of purl loops, whereas an nxm rib knit pattern alternates n columns of knit loops with m columns of purl loops. Initially, these columns lay flat in a nearly planar textile, however, the columns rotate relative to one another creating a series of connected planes in an accordion-like shape upon actuation, increasing the thickness of the textile and decreasing the width. The change in the leg position relative to the ridge creates angular movement resulting in an accordion shape.

A 2x2rib prototype (Figure 8d, e) was created using 15 mil wire, 5.5 mm needles and 10 loops for a prototype that measured 10 cm long. The prototype transforms from planar to a series of connected planes 45° to one another, reaching a height of 2.5 cm while reducing the width by 40% without change to the prototype length. The vertically striped knit pattern of rib creates a large distributed accordion-like motion that can provide controllable three-dimensional textures or act as an embeddable planar lift.

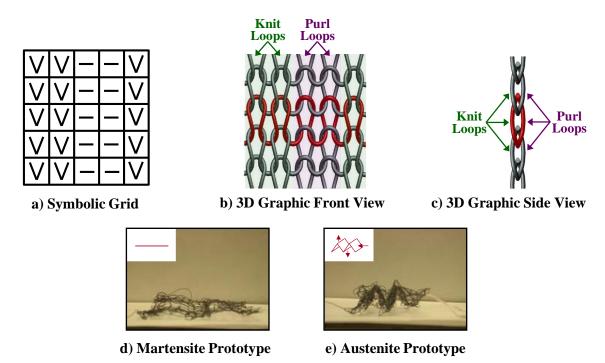


Figure 8. Vertically Striped Knit Pattern - Rib. The accordion-like actuation motion of rib is driven by the constrained asymmetric architecture. A 2x2 rib is shown with a) symbolic grid, b) a front view 3D graphic of alternating columns of knit and purl loops and c) a side view 3D graphic of columns with slight out-of-plane curvatures that alternate in different directions. The pictures demonstrate d) the flat prototype in the cold martensite state and e) the expanded accordion ridges of the prototype in the hot austenite state.

2.2.4. Diagonally Striped Patterns – Seed

Diagonally striped knit patterns are created with alternating diagonals of knit and purl loops in the knitting grid. One diagonally striped knit pattern is seed (Figure 9). The seed knit pattern is created by alternating single knit and purl loops in the first course and in the adjacent course single purl loops are alternated with single knit loops. This creates an alternating pattern that results in a textile with checkerboard-like surface of smooth forward loops and rear ridges. The planar textile transforms into a synclastically arching shape during actuation. The arching is a result of each loop contracting horizontally and vertically, causing the horizontally and vertically symmetric knit pattern to arch along the horizontal and vertical axes.

A seed prototype (Figure 9d, e) was produced with 5.5 mm needles using 15 mil wire with 10 loops for a total length of 9.5 cm. When heated the length and width of the prototype did not change but curved, creating a 180° arch. The diagonally striped knit loop pattern creates a domeshaped actuator that could be used to actively texture a surface or to produce gross three-dimensional reshaping of a surface.

2.3. LEVEL 3: GRID PATTERNS

The third level of the knit hierarchy, *grid patterns*, is composed of regions of knit patterns that are arranged spatially across the knitting grid to form more complicated, heterogeneous patterns. By varying the knit patterns used across the knitting grid, different motions can be produced over different regions of the textile. The more complicated architectures of the grid patterns provide enhanced complexity and increased variety of available three-dimensional shape

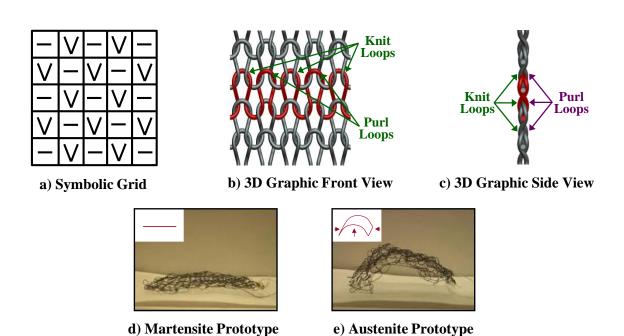


Figure 9. Diagonally Striped Knit Pattern – Seed. The synclastic arching of seed is driven by the checkerboard-like architecture that causes bending through the rows and columns. Shown are the a) symbolic grid, the b) front view 3D graphic of the checkerboard knit and purl loop pattern and the c) side view 3D graphic. The pictures demonstrate the d) flat prototype in the cold martensite state and e) synclastic arches of the prototype in the hot austenite state.

changing behaviors as compared to a homogeneous knit pattern. A grid pattern is formed by connecting multiple regions of knit patterns to create a knit textile that has different regions with varying knit loop patterns. More specifically, a grid pattern is created by connecting the edge loops of adjacent knit loop patterns to form a larger and more complex textile with regionally varied surface topologies. Combining different knit loop patterns into grid patterns constructs knit textiles that are capable of generating complex motions by producing different behaviors in different actuation areas.

The most basic combination knit loop pattern distribution is formed by synthesizing two knit loop patterns across a single textile (Figure 10). To demonstrate this, a prototype made using 10 mil wire and 7 mm needles with 8 loops was constructed of stockinette for 6 cm and rib for 6 cm (Figure 10b, c). The unique combination of the rib and stockinette knit loop pattern causes one side of the prototype to accordion while the other side flips over to cover the accordioned portion. Combining knit loop patterns in a knit loop pattern distribution is a powerful tool that produces textiles that create controllable complex three-dimensional motions distributed heterogeneously over an entire surface forming variable surface actuators.

2.4. LEVEL 4: RESTRUCTURED GRIDS

The fourth level of the hierarchical architecture, *restructured grids*, refers to how loops in the textile are connected in modified knitting grids. Knit patterns and grid patterns, which are created row-wise in a back-and-forth manner to form a grid of rows and columns of loops, are planar and rectangular. However, other textile shapes can be produced by connecting loops in non-orthogonal restructured knitting grids. Using restructured grids creates knitted structures with varied internal connections or modified boundary conditions and results in textiles that can be used to shape and leverage the mechanical behavior of the underlying knits, producing new

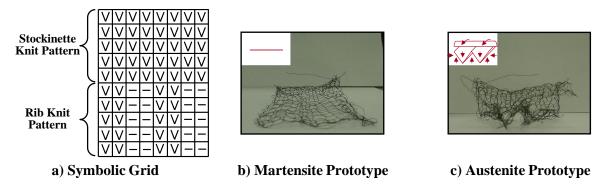


Figure 10. Grid Pattern. a) The symbolic grid shows a grid pattern composed of rib and stockinette knit patterns. In the cold martensite phase the textile is relatively flat (b); upon actuation half of the textile accordions and the other half flips over to cover the accordion portion (c). Combining knit patterns into a grid pattern creates distributed controllable three-dimensional motions.

behaviors and enhancing the kinematic performance. This section describes four ways of restructuring the grid – Post-Knitting Connections, Course-Wise Restructuring, Grid Cell Merging, and Re-Ordered Grids.

2.4.1. Post-Knitting Connection

Post-knitting connections are operations done on one or more knit textiles after the knitting process has been completed. Typically, post-knitting connections involve connecting two edges to one another, thus creating a three dimensional structure (much in the way a knitted garment is created from flat knit pieces). The act of connecting the edges bends the textile, which restructures the grid such that it is no longer composed of planar orthogonal rows and columns. The result of the restructured grid is a textile that has a structure that can further leverage the underlying behavior of the knit pattern or grid pattern used in the construction of the textile. While any edge of a textile could be connected to another edge of the same textile (top to bottom, left to right bottom to left, etc.), both of the examples given in this section use a top to bottom connection, which forms a belt.

The first example of a post-knitting connection is a stockinette belt (Figure 9a) which is created by joining the first and last course of a stockinette textile, forming a three-dimensional tube. Connecting the textile into a three-dimensional deployable structure allows the curvature of the stockinette courses to provide support in the wale-wise direction, lifting and lowering an applied load during actuation. A stockinette belt prototype (12 mil wire on 8 mm needles over 8 loops for 12 cm) was created by seaming the top and bottom of the planar textile to create a tube (Figure 9b, c). The knit structure is able to lift 1.8 N while expanding to four times its length and maintaining the same belt diameter. This connection is another set of boundary conditions that allows relatively little material to do a huge amount of work in a small package size. The knit architecture, working in a tubular structure, provides support to the otherwise flexible sheet, amplifying the intrinsic material strain by two orders of magnitude, while preserving its ability to produce useful forces.

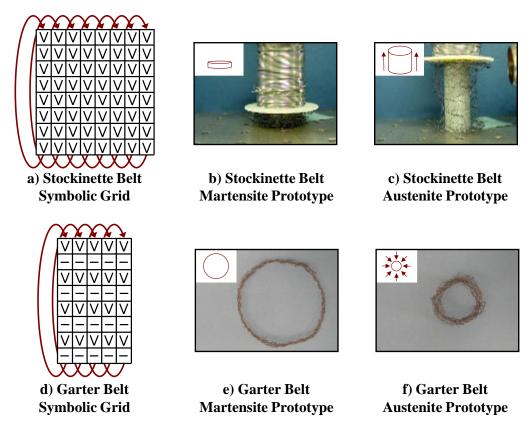


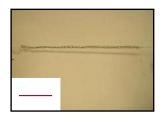
Figure 11. Restructured Grid – **Post-Knitting Connection**. Post-knitting connections can be used to create Active Knit belts. a) A stockinette grid pattern is connected along the top and bottom of the prototype to form a stockinette belt which b) actuates from the initially compressed martensite state to c) lift the applied load in the expanded austenite state. d) A garter grid pattern is connected along the top and bottom of the prototype to form a garter belt which e) actuates from the initially expanded cylinder in the martensite state to f) a contracted cylinder in the austenite state. The post-knitting connection restructures the knitting grid to form a structure that further leverages the kinematic behavior of the foundation knit pattern.

The second example of post-knitting connection is a garter belt (Figure 11d), which is created by joining the first and last course of a garter knit pattern textile. Connecting the ends transforms the textile from planar to tubular, inducing slight curvature along the length of the loops. Because the base knit pattern is garter, the primary motion of the belt is contraction. Joining the top and bottom edges of the contractile textile forms a belt that contracts in diameter during actuation. To demonstrate this, a garter knit pattern belt prototype was created from a textile made with 8 mil wire on 9 mm knitting needles over 5 loops until it was 25 cm long by connecting the first and last course of the textile (Figure 11e, f). The knit acted as a contractile belt reducing the diameter from 10.5 cm to 6 cm, reducing the cross sectional area of the belt by 67%, and slightly expanding the belt width. The connected garter structure could be used as a smart mechanical transmission belt or could be used as a parallel actuator to increase the load supported by the actuator.

2.4.2. Course-Wise Restructuring

Course-wise restructuring is an alternative knitting order that uses a restructured grid to connect the side edge loops across the textile during the knitting process (rather than after knitting as is the case for post-knitting connections) to form a three-dimensional structure (Figure 12). Course-wise restructuring is accomplished using circular knitting, a method in







a) Symbolic Grid

b) Martensite Prototype

c) Austenite Prototype

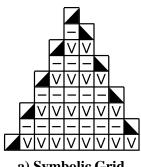
Figure 12. Restructured Grid – Course-Wise Restructuring. Course-wise restructuring can be used to create I-cord textiles. a) Courses of a stockinette grid pattern are restructured by helically knitting across the textile to form knitted tubes which actuate from b) long thin tubes in the martensite state to c) a helically coiled structure in the austenite state. Course-wise restructuring forms restructured grids that produce novel out-of-plane actuation behaviors.

which each course of knit loops are knit over the previous course creating a helical pattern of interlacing adjacent loops. The knit loops in course-wise restructured textiles are skewed (asymmetric) because a single course is helically connected as opposed to the orthogonal rows and columns of loops formed using simple orthogonal knitting grids. Active knits created using course-wise restructured grids produce three-dimensional textiles that are constrained by the helically connected knitted loops, and produce novel out-of-plane motions a result of the skewed, asymmetric knitted loops of the restructured grid.

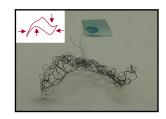
An I-cord is a type of textile that can be created using a course-wise restructured grid. Icords are created by circularly knitting with a single SMA fiber to create a long thin seamless three dimensional tube that provide simultaneous contraction and rotation upon actuation. Traditionally, I-cord textiles have a base knit pattern of stockinette. Stockinette I-cords are asymmetric about the inside and outside of the cylinder: The outside of the tube is smooth because of the forward loops (similar to the front of a stockinette knit pattern), while the inside of the cylinder has a continuous spiraling ridge (similar to the back of a stockinette knit pattern). For thinner I-cords, where each pass of the helix consists of a small number of loops, the straight knit tube spirals into a tight helix when actuated, increasing the diameter of the textile while reducing the length. As the individual loops are heated they shrink in height and increase in width. The width increase propagates through the textile altering the angle between knitted loops which creates the helical shape. An I-cord prototype (Figure 12b, c) was made by helically knitting 3 loops of 8 mil wire on 3 mm diameter needles using stockinette knit pattern until the prototype was 12 cm long. The 0.4 cm diameter seamless tube at room temperature spiraled to a maximum coil diameter of 1.4 cm while reducing in length by 85% when exposed to heat above the transition temperature. By restructuring the grid at the course-wise level, I-cord textiles provide extreme contraction at a point and act as a unique type of torque generator that can produce huge rotations in a very thin package.

2.4.3. Grid Cell Merging

Merging grid cells decreases the number of loops in a course, forming a restructured grid that results in textiles with complex, non-rectangular shapes (Figure 13). Decreasing the number of knitted loops in a course through grid cell merging is a technique often used in complex patterns to create three-dimensional draping textiles, as in the shoulder of a sweater. Active knits created using grid cell merging not only produce textiles with non-rectangular shapes, they







a) Symbolic Grid

b) Martensite Prototype

c) Austenite Prototype

Figure 13. Restructured Grid – Grid Cell Merging. Grid cell merging can be used to create triangular actuators. a) Courses of a garter grid pattern are manipulated by merging adjacent grid cells in alternating courses to form a triangularly shaped actuator. The triangular actuator actuates from b) the flat triangular shape in the martensite state to c) a contracted triangle with ends that curl in opposite directions due to the asymmetric boundary conditions in the austenite state. Grid cell merging restructures the grid to provide complex actuator shapes.

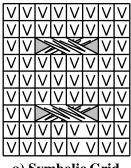
provide unique actuation motions unattainable by knit patterns or grid patterns alone. For example, a triangular textile is one possible textile shape that can be created using grid cell merging. Triangular textiles are created by decreasing the number of loops in each course by one. These decreases occur along the edges of the textile, modifying the boundary conditions. The added boundary condition modifies the behavior of the base knit pattern by constraining the edges to curl as two loops are twisted to occupy the same cell in the knitting grid.

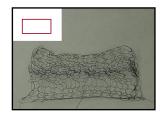
To demonstrate the kinematic behavior, a triangular textile was created (Figure 13b, c) using 10 mil wire and 6 mm needles with 20 loops. The textile was knit using the garter knit pattern and at the beginning of each course, two loops were knit together, decreasing the number of loops by one at the start of each course, creating a triangle with a height of 6 cm. Upon actuation, the height of the triangle decreases (characteristic of the garter knit pattern) and the two base corners curl, one upward and one downward. The legs bend in different directions because of the alternating boundary conditions, a result of knitting loops together in each course on alternating sides of the prototype. By controlling the boundary conditions though manipulation of the shape of the actuator, new complex three dimensional motions can be achieved and alternative complex actuator shapes are realized, neither of which have been possible through other actuation strategies.

2.4.4. Re-Ordered Grids

Re-ordered grids change the local connectivity of knitted loops within a knit textile (Figure 14). In knit patterns and grid patterns the row and column adjacency of the knitted loops is maintained. A re-ordered grid forms a restructured grid, modifying the connectivity of the rows and/or columns and resulting in loops that are crossed into different columns or loops that are stretched into different rows. One example of this is cabling, which is a method of attaching adjacent regions of knit pattern together by overlapping the edge loops of each adjacent pattern such that the order of two sets of columns in the earlier rows is reversed. The overlapping of the loops creates a torque within the textile causing it to twist about the vertical axis. This twisting occurs because the crossing of the loops pulls opposite corners of the textile toward one another, generating rotation about the length of the textile.

A cable was created by overlapping the four centermost loops in every 6th course of a textile made with a stockinette knit loop pattern. This cable prototype was made using 8 mil wire,







a) Symbolic Grid

b) Martensite Prototype

c) Austenite Prototype

Figure 14. Restructured Grid - Re-Ordered Grids. Re-ordered grids can be used to make cables in a knitted textile. a) The four innermost knit cells are overlapped (the two cells on the left are bent and stretched to the right and the two cells on the right are bent and stretched to the left). The cable actuator actuates from b) a flat rectangle in the martensite to c) a rectangle that is torqued along its length in the austenite state. Re-ordering the grid creates new motions unavailable with knit patterns alone.

5.5 mm needles, and 12 loops for a total of 10 cm (Figure 14b, c). The top of the rectangular prototype rotates clockwise about the vertical axis while the bottom rotates counterclockwise creating a tube. Reordering the cells within the knitting grid creates a restructured grid that produces tailorable motions that are not available from the basic knit loop patterns alone.

2.5. **ACTIVE KNIT HIERARCHY CONCLUSIONS**

This section leveraged the cellular hierarchical approach of traditional and engineering textiles to develop a more sophisticated classification of active knits that accounts for 1) multiple types of unit cells, 2) homogeneous distribution of unit cells across the knitting grid of the textile, 3) heterogeneous distribution of unit cells across the knitting grid of the textile, and 4) non planar orthogonal knitting grids. A four level hierarchy was introduced and experimental examples were provided to demonstrate the advancing complexity of actuation behaviors: knitted loops, knit patterns, grid patterns, and restructured grids. The first level of the hierarchical architecture, *knitted loops*, acts as the unit cell of the knitting grid and produces large strains as the bent loops leverage the strain of the foundational wire. The second level of the hierarchy, knit patterns, forms homogeneous patterns of adjacent knit and purl loops across the knitting grid that interact to provide three-dimensional actuation motions such as rolling, contraction, accordion, and arching. The third level, grid patterns, combines multiple knit patterns to form heterogeneous patterns across the knitting grid which affords complex and controlled three dimensional actuation motions across different areas of the textile such as arching in one area and accordioning in another. The fourth level, restructured grids, restructures the knitting grid by forming both uniquely shaped and three dimensionally structured textiles that leverage the behavior of knit patterns and grid patterns to provide new three-dimensional actuation motions distributed across a surface and throughout a structure such as deployable tubes, contractile belts, coiling tubes, triangular actuators, and twisting surfaces. This experimental survey of the actuation behavior of a variety of key active knit architectures at different hierarchal levels opens the door for a broader understanding of the actuation mechanism and gives a glimpse into the potential of this new architecture scheme. The language developed around the hierarchy provides a consistent basis through which a variety of architectures and their actuation behavior, application potential and impact, can be explored and discussed. For example, the hierarchy identified the basic unit as the knitted loop, and demonstrated the assembly of more complex

levels of textiles. Development of the hierarchical classification establishes a starting point for the derivation of models that provide a quantitative basis for the kinematic and kinetic performance of the knitted loop, and then an approach to build up textile models to capture the ever-increasing complex motion afforded by each level of the hierarchy. This kinematic active knit hierarchy study has shown that the basic architectural element, the knitted loop, has the potential to be transformed innumerable ways and may provide more novel complex distributed motions through the discovery of additional architectural manipulations.

3. TWO-DIMENSIONAL ANALYTICAL MODEL OF PLANAR ACTIVE KNITTED LOOPS

To advance active knit technology and establish the science base to implement the technology in applications, a model that captures the kinetic performance of active knitted textiles is needed. Active knits are complicated hierarchical structures; therefore, the first step in creating a predictive model is to model the kinetic behavior of the first level of the active knit hierarchy – the knitted loop. Knitted loops are assembled according to the knitting grid to create knit patterns; therefore, the kinetic performance of the individual loops is scaled in series and parallel to predict the performance of knit pattern active knit textiles. This section presents a model of the active knitted loop that predicts the kinetic actuation performance of a planar knitted loop and garter knit pattern active textiles.

Most existing knit models take a hierarchical modeling approach, which extrapolates the performance of a unit cell to predict the load-extension behavior of an entire textile. Even though several models exist for knitted loops, none of them includes active materials or the large deformation states created through activation. Geometric models of knitted loop combined to represent plain knit pattern apparel fabrics in their relaxed state have existed for most of the last century [61]-[67]. Other small-deformation models characterize the geometry of the knitted loop using the stitch density [68]-[69] and have been expanded to include the initial tension of the curved knitted loop [70]-[73]. More recently, materials knitted from glass, steel, and carbon fiber materials have been investigated for use within composites for their potential for improving energy absorption, bearing and notched strengths and fracture toughness [74]-[78]. Models that are more sophisticated [79]-[81] have been developed recently that take into account larger deformations of the knitted loop from engineering materials, represent expanded architectures, accept different stress profiles and look at the knit from a micromechanics point of view such as the bridging model, but they still use only traditional engineering materials and apply to only a few knit pattern architectures. While these existing models do not capture the motion of active knits, they do provide a starting foundation for modeling active knit actuators.

While existing passive knit models serve as a foundation for the kinetic modeling of active knits no existing models are capable of predicting the actuation performance of active knits. However, existing models can be modified and combined in order to capture the actuation behavior of active knits by including the thermal and mechanical operational transitions that occur during active knit actuation and including the influence of the load path and the interlacing loop friction. The first and most important modification is to incorporate the dual state nature of the active knits, which no existing knit models capture. The actuation motion produced by active knits is a result of the material transformation between stiff austenite phase and the flexible, less stiff martensite phase. An active knit model must incorporate the dual stiffness material behavior of the active material. Because active knits cycle between states incorporating friction between interlacing adjacent loops is essential. Most existing models neglect friction between adjacent loops and the few models that include friction only predict the extension of the knitted loop under load. Adjacent loops of active knits stick or slip past one another as they cycle between extended and contracted states depending on the motion direction and loading history. The varying states of friction are not covered in any existing models and must be included in an active knit model to accurately predict the hysteresis due to friction. By modifying and combining existing passive knit models, particularly those developed by Hong [74] and Shanahan [73], a quasi-static analytical model is developed that predicts the actuation of the

active knit based on the state it is in, the state it came from, and the inter-loop friction experienced during the operational transition into the state.

This section presents an analytical state-based actuation model of the planar knitted loop in the garter knit pattern fabricated from variable stiffness smart material wire which accounts for the loading path and the friction between interlacing adjacent loops. The states of operation are defined based on the mechanical loading of the textile, the transition between different material stiffness, and the paths followed to arrive at each state. Operational transitions between these states induce frictional forces (stick or slip) depending upon the state and path, which affect the actuation response. A load-extension model is derived for each state of a typical actuation cycle with respect to the unit cell of a single loop of the textile based on the stress-strain behavior of the active material with assumptions made to allow analytical tractability. Elastica Theory and Euler-Bernoulli beam bending are used to capture the large deformations within a loop of wire. The resulting kinematic and kinetic relations for a single cell scale the load-extension behavior of the entire knit textile for each state, and provide analytical algebraic transcendental expressions for the net actuation motion as a function of the applied tensile load on the textile. The model is validated experimentally for a thermally actuated SMA garter knit prototype over a range of applied forces with good correlation. The two dimensional analytical active knit loop model provides the ability to predict actuation motions for the radical stroke and force garter knit pattern actuation architecture, enabling the design of active knitted architectures for a wide range of applications.

3.1. Nomenclature

| 2121 | |
|-------------------------------|--|
| A | Inflection point at end of loop leg |
| В | Interlacing contact point |
| C | Point at top of loop |
| C | Course height |
| C_1 , C_2 , C_3 , C_4 | Functions of angles used to simplify notation |
| D | Center of the unit cell |
| D | Knitting needle diameter |
| d | Wire diameter |
| E | Elliptic integral of the second kind |
| E_A | Base material Austenite Young's modulus |
| E_M | Base material Martensite Young's modulus |
| \hat{E}^{m} | Difference between complete and incomplete Elliptic integrals of the second kind |
| F | Elliptic integral of the first kind |
| F_{app} | Externally applied force to knit textile |
| F_{loop} | Externally applied force to knit loop |
| F_{UC} | Externally applied force to unit cell |
| \hat{F} | Difference between complete and incomplete Elliptic integrals of the first kind |
| I | Second moment of inertia of wire cross-section |
| k_1, k_2 | Geometric functions of angles used in elliptic integrals |
| L | Knit loop length |
| $L_{subscript}$ | State dependent length of knit textile |
| M | Bending moment at top of loop |
| | |

 N_c

 N_{W}

0

Number of courses in knit textile

Reaction force at end of loop leg

Number of wales in knit textile

Unit cell origin

| R | Reaction force at interlacing contact point |
|---|---|
| S T | Length along loop Horizontal wire tension at top of loop |
| \overline{W} | Wale width |
| X, Y | Global coordinate system |
| <i>x</i> , <i>y</i> | Local coordinate system for segment BC |
| x',y' | Local coordinate system for segment AB |
| α | Loop state angle of the connecting leg at A |
| β | Loop state angle of the reaction force between adjacent loops |
| Δ | Knit textile deflection |
| δ | Unit cell deflection |
| $\mathcal{E}_1, \mathcal{E}_{2,}$ | Geometric functions of angles used in elliptic integrals |
| $\varphi_{1B}, \ \varphi_{2B}$ γ | Loop state angle of force P at A |
| μ | Coefficient of friction between interlacing loops |
| θ, θ' | Deflection angle along loop |
| <u>Subscripts</u> | |
| A | Austenite phase |
| ACT | Actuator |
| cont | Contracted state |
| ext | Extended state |
| M | Martensite phase |
| 0 | Initial state with zero external load |

3.2. GARTER KNIT PATTERN ARCHITECTURE AND OPERATION

Garter knit pattern textiles generate large distributed planar contractile actuation motions as a result of their symmetrical loop architecture. The symmetric knit pattern actuator undergoes a four state operational procedure that results in a constant load actuation cycle. The unique garter knit pattern architecture and multi-state operation are described in this section.

3.2.1. Garter Knit Pattern Architecture

The architecture of a knit pattern is defined by the arrangement of knit and purl connections between interlaced loops of adjacent courses (Figure 16). A course is a row of knit loops, shown in red in Figure 16, which is composed of a single strand of alternating (up and down) curved loops. A wale is a column of knit loops, the legs of each loop interlocking with the top of the next loop down the wale (i.e. in the next course). In a knit connection, the legs of the upper loop in a wale overlap the top of the lower loop in the same wale and interlace behind the sides of the loop, whereas in a purl connection the top of the lower loop overlap the legs of the upper loop which interlace behind the sides of the lower loop. The ordering of the knit and purl connections define the knit pattern architecture where the garter knit pattern, composed of alternating courses of all knit and all purl connections, forms a planar textile symmetric about the front and back. The loops within the garter knit pattern architecture provide large curvatures through which loops interlace with the adjacent loop making contact at the interlacing contact point, B. The interlacing contact point may change position as adjacent loops slip relative to each other against friction, depending on the relative magnitudes of the loading and contact forces and the coefficient of friction between the wires. The garter knit is geometrically defined by its course

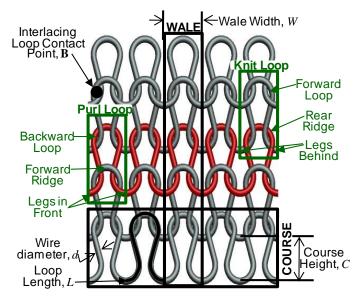


Figure 15. Basic Garter Knit Pattern Architecture. Forward knit loops and backward purl loops make up courses (rows of loops) and wales (columns of loops), characterized by the course height (C), wale width (W), wire diameter (d), and loop length (L).

height (C), wale width (W), loop length (L), and fiber diameter (d). The course height (C) is the vertical distance between identical reference points of adjacent rows. The wale width (W) is the horizontal distance between identical reference points on adjacent loops within a course. The loop length (L) is the length along the centerline of the fiber of a single knit loop. The fiber diameter (d) is the diameter of the foundational wire.

3.2.2. Garter Knit Pattern Operation

SMA garter knit textiles go through *operational transitions* from one state to another resulting in a change in length and stiffness of the textile. The operational transitions are initiated by either a change in thermal loading, inducing a *material transition* from flexible Martensite to stiff Austenite, or by changes in mechanical loading. During these operational transitions, different friction conditions occur between loops of the knit (stick or slip) depending on the loading and the initial state. The state of the textile is defined by the thermal loading (Austenite or Martensite), the mechanical loading and the loading path by which the textile arrived into that *State* (*Free, Extended*, or *Contracted*). A typical actuation cycle (depicted in Figure 16) is initiated from the *Austenite Free State* with an operational transition into the *Austenite Extended State*, and then cycles between the *Martensite Extended State* and the *Austenite Contracted State*. The length of the textile in each state, and therefore the motion produced by each operational transition, depends on four factors: 1) the state it is in, 2) the state it came from, 3) the magnitude of the mechanical loading, and 4) the inter-loop friction conditions experienced during operational transition into its state.

3.2.2.1. Austenite Free State

A typical actuation cycle is initiated with the SMA garter knit textile in a heated state with no external loads. When the temperature of the SMA is raised above its Austenite Finish transition temperature, it makes a material transition from a soft Martensite phase to a stiff Austenite phase. In transitioning, deformations experienced in the Martensite state are recovered,

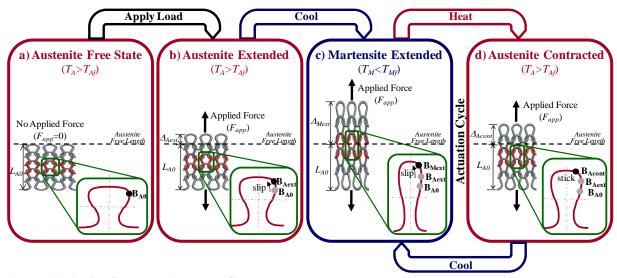


Figure 16. Active Garter Knit Pattern States. a) Austenite Free State, b) Austenite Extended State, c) Martensite Extended State, and d) Austenite Contracted State reached through thermal or mechanical operational transitions where a typical actuation cycle is alternates between the Martensite Extended and Austenite Contracted States.

producing the Shape Memory Effect of SMA. While the material phase of SMA is a function of both temperature and stress, for modeling purposes, it is assumed that a complete thermal transition occurs throughout the wire and that the bending stresses are low enough such that no areas of stress induced martensite are developed. Because the Martensite strains are recovered, the Austenite Free State provides a zero reference for computing material strains. In a knitted structure, however, the material is not actually in a zero-strain state since the wires, which come from the manufacturer trained to a straight shape, are bent in loops. When heated they attempt to return to their naturally straight configuration resulting in a relatively wide wale width, W, and a relatively short course height, C. Even though many internal stresses and strains exist, the garter knit textile length L_{A0} in the Austenite Free State (Figure 16a) is set as the zero deflection reference point for actuation.

3.2.2.2. Austenite Extended State

When a tensile load, F_{app} , is applied to the textile in this heated state, the knit loops elongate, increasing the course height C, and lengthening the entire textile by a deflection Δ_{Aext} , relative to the Austenite Free length, L_{A0} . During this operational transition into the Austenite Extended State (Figure 16b), the adjacent loops of wire generally slip past each other from an initial point of contact \mathbf{B}_{A0} along the loop to a final interlacing contact point \mathbf{B}_{Aext} . The resulting friction resists the slip and therefore resists elongation of the textile, reducing the deflection Δ_{Aext} into this state.

3.2.2.3. Martensite Extended State

When the textile is allowed to cool under load to a temperature below its Martensite Finish transition temperature, the textile makes a material transition into the Martensite phase and becomes less stiff. It is assumed that the stiffness decreases as a result of a complete thermal transition as all the material cools below the Martensite finish temperature. As a result, the course height of the loops elongates further into the Martensite Extended State (Figure 16c) in which the textile is deflected by Δ_{Mext} relative to the Austenite Free length, where $\Delta_{\text{Mext}} > \Delta_{\text{Aext}}$.

During this operational transition, adjacent loops slip further past each other from the Austenite Extended interlacing point of contact \mathbf{B}_{Aext} , to the Martensite Extended interlacing point of contact \mathbf{B}_{Mext} such that friction again reduces the deflection experienced by the textile during this operational transition. The Martensite Extended State is the first of two states in the cyclic portion of the typical actuation cycle.

3.2.2.4. Austenite Contracted State

The next state of the actuation cycle is entered when the material is heated under load to above its Austenite Finish transition temperature to the Austenite phase. The resulting stiffening of the material causes the wires within each loop to attempt to straighten to their natural straight shape, reducing the course height, and inducing contraction of the textile to a length deflected from the Austenite Free length by a distance Δ_{Acont} , where $\Delta_{Mext} > \Delta_{Acont} > \Delta_{Aext}$. During this operational transition into the Austenite Contracted State (Figure 16d), friction between the loops opposes relative motion of the interlacing point of contact back downward toward the Austenite Extended interlacing point of contact \mathbf{B}_{Aext} . In most cases, the friction is observed to completely block slippage such that the Austenite Contracted interlacing point of contact \mathbf{B}_{Acont} remains stuck at the Martensite Extended interlacing point of contact \mathbf{B}_{Mext} . Thus, even though the thermal and mechanical loading are identical in the Austenite Extended State and the Austenite Contracted State, the length in the Austenite Contracted State is longer than that of the Austenite Extended State due to the change in direction and stick-slip nature of the friction conditions experienced in arriving at each state.

Actuation against an applied force F_{app} occurs cyclically between the Austenite Contracted State and the Martensite Extended State, where the net actuation deflection Δ_{ACT} is equal to the difference between the Martensite Extended deflection and the Austenite Contracted deflection $(\Delta_{ACT} = \Delta_{Mext} - \Delta_{Aext})$.

3.3. ANALYTICAL GARTER KNIT PATTERN MODEL

An analytical state-based actuation model is derived for the garter knit pattern architecture to predict the load-extension behavior of each state and net actuation motion as a function of the applied tensile load on the textile, thermal load and material phase, and path dependent friction. While several load-extension models exist for passive textile knits [61]-[81], they do not model the multi-state contractile actuation of active knits. Existing knit models are typically purely geometric and only capture small deformations, while engineering models that account for larger deformations only predict the load-extension behavior of a passive single-state knit. None of these existing models incorporate thermal and mechanical operational transitions from one state to another, and they all neglect the influence of the load path and the interlacing loop friction.

These passive knit models however, do provide a starting foundation for the modeling of the load-extension of individual states of an active knit. By modifying and combining existing passive knit models, particularly those developed by Hong [74] and Shanahan [73], a quasi-static analytical model can be developed that predicts the actuation of the active knit based on the state it is in, the state it came from, and the inter-loop friction experienced during the operational transition into the state. The required modifications include incorporating slipping and sticking between adjacent interlacing loops, enforcing compatibility of displacements and curvature at the interlacing contact point, and accounting for the change in stiffness between states.

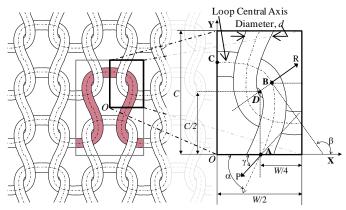


Figure 17. Knit Unit Cell. The knit unit cell is one quarter of a knit loop (shown in red) and is defined by geometric parameters (course height - C, wale width - W, loop length - L, wire diameter - d) and unknown characteristic angles (α , β , and γ).

The modeling approach uses a quarter of the knit loop as the unit cell of the garter knit pattern architecture. Geometric relations are established for the unit cell taking advantage of the high level of symmetry within the structure to describe the position of key points and inflections within the cell. The reference Austenite Free State is modeled to establish the base geometry and loop shape, as well as the load-extension behavior of the Austenite and Martensite Extended, and the Austenite Contracted States. For each state, the shape of the loop is established using Elastica Theory and Euler-Bernoulli beam bending to capture the large bending rotations using a small-strain linear deflection approximation of the SMA wire in each phase. Equilibrium equations are developed for the loop including the stick or slip friction interaction between loops depending on the particular operational transition. The resulting governing differential equations are integrated along the loop using boundary conditions derived from geometry to provide a set of algebraic equations relating a set of three unknown loop state angles to the overall size of the cell. Kinetic relations for each state are formulated to relate the loading on each loop to its shape providing fully analytical transcendental equations from which the load-extension behavior of the unit cell is derived. The difference between the load-extension behavior of the Martensite Extended and Austenite Contracted States describes the actuation behavior of the unit cell. The unit cell properties are scaled by the numbers of courses and wales to provide the load-extension behavior and net actuation behavior of the entire knit textile.

3.3.1. Assumptions

To simplify the modeling approach and to enable analytical tractability, several assumptions about the fibrous active material and loop architecture are employed. The fiber is assumed to be a naturally straight, inextensible, incompressible, homogeneous, elastic rod that experiences the shape memory effect. The SMA wire is assumed to be trained to a straight shape that is recoverable upon heating at low load levels. While inextensibility is not traditionally associated with SMA wire because of its large axial extension and contraction capability, it is used in the knitted model because at typical load levels the extension of the knit is assumed to be governed by the change of shape in the knit loop caused by bending. The inextensibility assumption implies a constant diameter for the SMA wire.

The effective modulus of elasticity is phase dependent (E_A , E_M), assuming the material fully transforms between states as discussed in the operation section, and is derived from small strain

limiting cases of the nonlinear stress-strain relationships. In reality, the bending curvatures of the SMA material may not allow complete transformation into the austenite phase and a portion of the material may be in the stress induced martensite phase. Also, while linear elastic assumptions apply well to the full austenite state they only apply to the martensite state for small strains. However, these simplified material assumptions are made to enable tractability of the analytical model, and they do apply to situations with relatively large loop to wire diameter ratios, therefore to more loosely knit architectures.

In addition to assumptions about the fibrous material several loop architecture assumptions have been implemented. Every loop in the knitted textile is assumed to have the same planar geometry with no out of plane behavior during deformation. Interlacing loops from adjacent courses are assumed to always be in contact and the central axes of these loops are separated by one wire diameter (Figure 17). A simplified fiber reaction force, R, acting at a single point between the interlacing fibers perpendicular to the fiber axis is assumed while a frictional force, μR , acts at the same point along the fiber in the opposite direction of the sliding motion.

3.3.2. Geometric Relations

Geometry plays a crucial role in the development of an analytical model of active knitted material because it allows for the establishment of physical constraints between the known geometric parameters (course height-C, wale width-W, loop length-L, and wire diameter-d) and the unknown loop state angles (α , β , and γ). The three angles (the angle of the reaction force (R) between adjacent loops – β , the angle of the connecting leg at $A - \alpha$, and the angle of force P at $A - \gamma$) describe the geometric loop shape under different loads. The undetermined loop state angles vary during loading to allow for the direction of internal forces to change and slipping of the interlacing contact point during extension. The geometric constraints are developed by analyzing a unit cell of the garter knit pattern architecture. The unit cell is one quarter of the knit loop and a quarter of the interlacing adjacent loop (Figure 17). A complete knit loop can be assembled using symmetry by rotating and reflecting the unit cell about the X and Y-axes defining the origin at this center of symmetry, **O**, and matching the connection points at the top (or bottom) of the loop at C and at the end of the connecting leg at A. Symmetry dictates the position and curvature at point A. To ensure compatibility of displacements along the length of the wire A must be located in the bottom center of the unit cell at (0, W/4). Continuity requires A to be an inflection point acting along the angle α , because the direction of the curvature of the wire in the knit loop changes therefore A cannot support a moment. From A the wire begins to curve upward until it reaches the interlacing contact point **B**, the point along the central axis of the knit loop through which the resultant force between adjacent loops acts. To maintain symmetry, the line of action of the resultant force, R, which acts perpendicular to the tangent line at **B**, must pass through the center of the unit cell, **D**, located at (W/4, C/2) and representing the point of interaction between adjacent loops, requiring **B** to lay a distance of d/2 from **D** along an angle of β - $\pi/2$. From **B**, the foundational wire continues to curve toward the top of the knit loop, point C, located at an unknown height along the left-most edge of the unit cell.

Four different geometric relations can be derived from the unit geometry. The first geometric constraint,

$$\frac{W}{4} = X_B - \frac{d}{2}\cos\left(\beta - \frac{\pi}{2}\right),\tag{1}$$

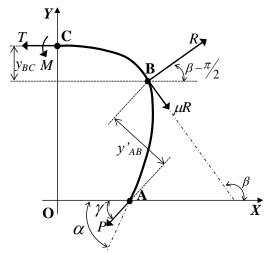


Figure 18. Garter Knit Unit Cell Free Body Diagram. The Free Body Diagram includes the internal forces and moments -T, R, μR , P, and M and the loop state angles (α , β , and γ)..

relates X_B , the X-coordinate of the interlacing contact point, **B**, to W/4, the X position of point **A**, using the assumption that the adjacent interlocking wires are in contact and incompressible, therefore separated by the wire diameter, d, along the line of action of R. Similarly, a second constraint,

$$X_B - X_A = \frac{d}{2}\cos\left(\beta - \frac{\pi}{2}\right),\tag{2}$$

couples the difference in the X-coordinates of the interlacing contact point and leg end, X_B and X_A , to the horizontal component of the distance between the loop interaction point, \mathbf{D} , and half the wire diameter. Using the same assumptions as used for the development of wale width constraint (Equation 1), a third constraint,

$$\frac{C}{2} = Y_B - \frac{d}{2}\sin\left(\beta - \frac{\pi}{2}\right),\tag{3}$$

associates the Y-coordinate of point **B**, with the vertical location of the center of the unit cell, C/2, using the wire diameter, d, and angle, β . The final geometric constraint,

$$\frac{L}{4} = s_{AB} + s_{BC} \tag{4}$$

is a compatibility equation relating the length of wire in the loop, L, to the combined length of segment **AB**, s_{AB} , and length of segment **BC**, s_{BC} , in this quarter knit loop established using the inextensibility assumption.

3.3.3. Austenite Free Reference State

The Austenite Free State acts as a reference state upon which all further calculations are made. The state is developed by analyzing the force equilibrium interactions and the governing differential equations for the segment of the loop above and below the interlacing contact point. The analysis allows for kinematic loop state equations to be derived in terms of measureable geometric parameters (course height -C, wale width -W, loop length -L, wire diameter -d)

and unknown loop state angles (α , β , and γ) which can be solved to provide the loop state angles. Once the loop state angles are known, the corresponding kinetic information (internal forces) can be calculated. The kinematic and kinetic values provide a reference state for the extension and contraction of the knitted structure.

3.3.3.1. Force Equilibrium Interactions

The free body diagram of the planar knit loop (Figure 18) is separated into two segments at the interlacing contact point (**B**) by the resultant force, R, transmitted by the adjacent interlocking loop. A friction force, μR , acts perpendicular to R at **B** in the positive X and negative Y direction to resist extension from the as-knit geometry which typically has more overlap and slack between courses. A single force P acts on point **A** at an angle of γ relative to the X-axis, which is an inflection point and cannot support a moment. At point **C**, a horizontal force, T, acts in the negative X-direction and a bending moment, M, acts counterclockwise (no shear can be supported due to symmetry).

Force-equilibrium analysis in the X and Y forces and moments provides kinetic loop relationships. Force equilibrium in the X-direction results in

$$T = R(\sin(\beta) - \mu\cos(\beta)) - P\cos(\gamma)$$
(5)

Equilibrium in the *Y*-direction produces

$$R = \frac{-P\sin(\gamma)}{\mu\sin(\beta) + \cos(\beta)},\tag{6}$$

which can be combined with the tension in the top of the loop from the X-direction equilibrium (Equation 5) to eliminate R and give the relationship

$$T = -P \left(\sin(\gamma) \frac{\sin(\beta) - \mu \cos(\beta)}{\cos(\beta) + \mu \sin(\beta)} + \cos(\gamma) \right)$$
(7)

For future simplification the substitution

$$k_{1} = \sin(\gamma) \frac{\sin(\beta) - \mu \cos(\beta)}{\cos(\beta) + \mu \sin(\beta)} + \cos(\gamma)$$
(8)

is made, where k_1 is a function of the geometric angles β and γ only.

The moment balance about **B** is

$$M = Py'_{AB} - Ty_{BC} \tag{9}$$

and can be simplified to

$$M = P\left(y'_{AB} + k_1 y_{BC}\right) \tag{10}$$

using the modified equation for the tension in the top of the loop (Equation 7), where y'_{AB} is the perpendicular distance between the line of action of P and B and y_{BC} is the vertical distance between B and the top of the loop, C.

3.3.3.2. Analysis of Governing Differential Equations

The governing differential equations describing the bending of the knit loop are developed using Elastica theory and Euler-Bernoulli beam bending. Elastica Theory is a theory of solid mechanics that accounts for large elastic rotations of structures during bending or buckling [76]. The use of Elastica Theory requires manipulation of the governing differential equations using the relations $dx/ds=cos(\theta)$ and $dy/ds=sin(\theta)$ to obtain closed form solutions involving complex elliptic functions. Bending of the knit unit cell is analyzed in two sections, segments **AB** and **BC**, while imposing continuity of displacements and slopes at **B**.

3.3.3.2.1. Lower Loop Segment AB

Segment AB is treated as an elastic rod pinned at A with an applied end load, P, and analyzed using a transformed coordinate system (x',y') centered at A where x' is along but opposite the line of action of P (Figure 19a). The differential equation describing this portion of the loop is simply

$$\frac{d\theta'}{ds} = \frac{Py'}{E_A I} \tag{11}$$

as determined from Euler-Bernoulli beam bending where θ' is the angle with the x'-axis, s' is the length along the loop, E_A is the phase dependent effective elastic modulus of the wire in the austenite phase, and I is the second moment of inertia of the wire cross section.

The governing differential equation for segment **AB** (Equation 11) is differentiated and the Elastica relation $dy/ds = sin(\theta)$ is used to obtain

$$\frac{d^2\theta'}{ds^2} = \frac{P}{E_A I} \frac{dy'}{ds} = \frac{P}{E_A I} \sin(\theta') \tag{12}$$

This equation is multiplied by $d\theta/ds$ and rearranged, giving

$$\frac{d}{ds} \left[\frac{1}{2} \left(\frac{d\theta'}{ds} \right)^2 + \frac{P}{E_A I} \cos(\theta') \right] = 0$$
(13)

which can be integrated to determine the length of the wire, s_{AB} , using the boundary conditions derived from geometry and the fact that point **A** is an inflection point

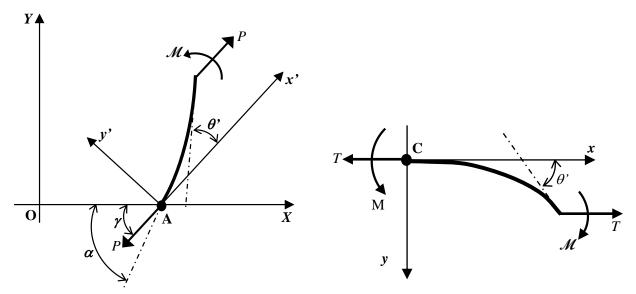
$$\theta'|_{s=0} = \alpha - \gamma \tag{14}$$

$$\left. \frac{d\theta'}{ds} \right|_{s=0} = 0$$
, and (15)

$$\theta'|_{s=s_{AB}} = \beta - \gamma \tag{16}$$

Two substitutions,

$$u = \cos\left(\frac{\theta'}{2}\right) \text{ and } \tag{17}$$



a) Free Body Diagram for Segment AB
b) Free Body Diagram for Segment BC
Figure 19. Loop Segment Free Body Diagrams. Free Body Diagrams for analysis of the governing differential equations of a) Segment AB and b) Segment BC.

$$z = \arcsin\left(\frac{u}{\cos\left(\frac{\alpha - \gamma}{2}\right)}\right),\tag{18}$$

are useful to manipulate the integral into a closed for elliptic integral describing the length of segment AB,

$$s_{AB} = \sqrt{\frac{E_A I}{P}} \hat{F}\left(\varepsilon_1, \varphi_{1B}\right), \tag{19}$$

where

$$\varepsilon_1 = \cos\left(\frac{\alpha - \gamma}{2}\right),\tag{20}$$

$$\varphi_{1B} = \arcsin\left(\cos\left(\frac{\beta - \gamma}{2}\right) / \cos\left(\frac{\alpha - \gamma}{2}\right)\right)$$
, and (21)

$$\hat{F}\left(\varepsilon_{1}, \varphi_{1B}\right) = F\left(\varepsilon_{1}, \frac{\pi}{2}\right) - F\left(\varepsilon_{1}, \varphi_{1B}\right) \tag{22}$$

given $F(\varepsilon_l, \pi/2)$ is a complete elliptic integral of the first kind and $F(\varepsilon_l, \phi_{lB})$ is an incomplete elliptic integral of the first kind. The curvature, $d\theta/ds$, at any point along the length of segment **AB** is found by differentiating the length along the loop (the general form of Equation 19) with respect to θ to obtain the equation

$$\frac{d\theta}{ds}\big|_{s=s_{BC}} = 2\varepsilon_1 \sqrt{\frac{E_A I}{P}} \cos(\varphi_{1B})$$
(23)

Integrating the combination of the Elastica assumptions and the curvature relationship (Equation 23) the x' and y' coordinates for loop segment AB are determined to be

$$x'_{AB} = \sqrt{\frac{E_A I}{P}} \left\{ \hat{F}\left(\varepsilon_1, \varphi_{1B}\right) - 2\hat{E}\left(\varepsilon_1, \varphi_{1B}\right) \right\}$$
 and (24)

$$y'_{AB} = 2\sqrt{\frac{E_A I}{P}} \varepsilon_1 \cos(\varphi_{1B}), \tag{25}$$

where

$$\hat{E}(\varepsilon_{1}, \varphi_{1B}) = E(\varepsilon_{1}, \frac{\pi}{2}) - E(\varepsilon_{1}, \varphi_{1B}), \qquad (26)$$

and $E(\varepsilon_l, \pi/2)$ is a complete elliptic integral of the second kind and $E(\varepsilon_l, \phi_{lB})$ is an incomplete elliptic integral of the second kind. Transforming the coordinate system from the local x', y' to the global X, Y through the angle γ results in

$$X = \frac{W}{4} + x'\cos(\gamma) - y'\sin(\gamma)$$
 and (27)

$$Y = x'\sin(\gamma) + y'\cos(\gamma) \tag{28}$$

The analysis of the lower loop segment **AB** provides half the fundamental equations used in determining the loop state angles.

3.3.3.2.2. Upper Loop Segment BC

Segment BC is treated as an elastic rod clamped at \mathbb{C} with a horizontal load, T, and an applied moment, M, while \mathbb{B} is free to move (Figure 19b) but must satisfy continuity conditions with AB. Segment BC is analyzed using the transformed coordinate system (x,y) where x is shifted vertically from X, C acts as the origin, and y acts in the negative Y direction. The differential governing equation for segment BC is given by

$$\frac{d\theta}{ds} = \frac{Ty + M}{E_A I} \,, \tag{29}$$

where θ is the angle between the x-axis and the tangent line to the loop. The modified equation for the tension in the top of the loop (Equation 7) and the moment at the top of the loop (Equation 10) are substituted into the governing differential equation for segment **BC** (Equation 29), which is differentiated and the Elastica relation is employed resulting in the manipulated equation

$$\frac{d}{ds} \left[\frac{1}{2} \left(\frac{d\theta}{ds} \right)^2 + \frac{T}{E_{A,M} I} \cos(\theta) \right] = 0$$
(30)

The differentiated governing differential equation (Equation 30) can be integrated to determine the length of the wire, s_{BC} , in segment **BC** using the geometric boundary conditions

$$\theta|_{s=0} = 0, \tag{31}$$

$$\theta \mid_{s=s_{BC}} = \pi - \beta$$
, and (32)

$$\frac{d\theta}{ds}|_{s=s_{BC}} = 2\varepsilon_1 \sqrt{\frac{E_A I}{P}} \cos(\varphi_{1B}), \tag{33}$$

where the boundary condition for the curvature at the interlacing contact point $\bf B$ (Equation 33) enforces continuity of wire curvature at $\bf B$. Employing the substitutions

$$u = \cos\left(\frac{\theta}{2}\right) \text{ and } \tag{34}$$

$$z = \arccos(u) \tag{35}$$

this integration results in an equation describing the length of segment BC,

$$s_{BC} = \sqrt{\frac{E_A I}{P}} \sqrt{\frac{2}{k_1 + k_2}} F\left(\varepsilon_2, \varphi_{2B}\right), \tag{36}$$

where

$$\varphi_{2B} = \frac{\pi - \beta}{2} \tag{37}$$

$$\varepsilon_2 = \sqrt{\frac{2k_1}{k_1 + k_2}}, \text{ and}$$
 (38)

$$k_2 = 2\varepsilon_1^2 \cos^2(\varphi_{1B}) + k_1 \cos(\beta), \tag{39}$$

and $F(\varepsilon_2, \phi_{2B})$ is an incomplete elliptic integral of the first kind. The x and y coordinates of **B** can be determined to be

$$x_{BC} = \sqrt{\frac{E_A I}{P}} \sqrt{\frac{2}{k_1 + k_2}} \left(\frac{2}{\varepsilon_2^2} E\left(\varepsilon_2, \varphi_{2B}\right) + \left(1 - \frac{2}{\varepsilon_2^2}\right) F\left(\varepsilon_2, \varphi_{2B}\right) \right) \tag{40}$$

and

$$y_{BC} = \sqrt{\frac{E_A I}{P}} \sqrt{\frac{2}{k_1 + k_2}} \left(\frac{-2}{\varepsilon_2^2} \left(\sqrt{1 - \varepsilon_2^2 \cdot \sin^2(\varphi_{2B})} - 1 \right) \right)$$
(41)

using the Elastica criteria. No coordinate transformation is needed for the x-coordinate but the equation

$$Y = Y_{AB} + (y_{BC} - y) \tag{42}$$

transforms any local coordinate y into a global coordinate Y.

3.3.3.3. Kinematic Relations

The kinematic equations developed during the analysis of the knit unit cell provides a set of nonlinear algebraic loop state equations that relate the initially measurable geometric parameters: wale width (W), course height (C), wire diameter (d), and loop length (L), to the unknown loop state angles. During the *Austenite Free State*, when no external load is applied to the knit unit cell, the loop state equations can be solved to obtain the loop state angles and the internal forces can be calculated.

The geometric constraints (Equations 1-4) can be modified with the new definitions of the coordinates and loop length segments (Equations 19, 27, 28, 36, and 40) in terms of the unknown loop state angles (α , β , and γ) and manipulated to eliminate the unknown force P to obtain the three loop state equations:

$$\frac{L}{W} = \frac{C_4}{C_1 - C_3} \tag{43}$$

$$\frac{L}{C} = \frac{2C_4}{C_2 + C_3 \cot(\beta)}, \text{ and}$$
(44)

$$\frac{L}{d} = \frac{2C_4 \sin(\beta)}{C_3},\tag{45}$$

which relate the geometric parameters (W, C, L, and d), which can be measured from any loop in the *Austenite Free State* of the knit textile, to the unknown loop state angles. The three algebraic loop state equations provide a set of simultaneous nonlinear equations where the C_i 's are only functions of α , β , and γ and are given by

$$C_{1} = \sqrt{\frac{2}{k_{1} + k_{2}}} \left[\frac{2}{\varepsilon_{2}^{2}} E(\varepsilon_{2}, \varphi_{2B}) + \left\{ 1 - \frac{2}{\varepsilon_{2}^{2}} \right\} F(\varepsilon_{2}, \varphi_{2B}) \right], \tag{46}$$

$$C_2 = \sin(\gamma) \{ f(\varepsilon_1, \varphi_{1B}) - 2e(\varepsilon_1, \varphi_{1B}) \} + 2\varepsilon_1 \cos(\gamma) \cos(\varphi_{1B}), \tag{47}$$

$$C_3 = \cos(\gamma) \{ f(\varepsilon_1, \varphi_{1B}) - 2e(\varepsilon_1, \varphi_{1B}) \} - 2\varepsilon_1 \sin(\gamma) \cos(\varphi_{1B}), \text{ and}$$
(48)

$$C_4 = f\left(\varepsilon_1, \varphi_{1B}\right) + \sqrt{\frac{2}{k_1 + k_2}} F\left(\varepsilon_2, \varphi_{2B}\right) \tag{49}$$

By making the initial material assumptions, the set of nonlinear differential equations was reduced to a set of three simultaneous transcendental algebraic equations. Using the measured geometric parameters, the system of loop state equations (Equations 43-45) can be solved numerically to determine the unknown loop state angles (α , β , and γ) that describe the unloaded loop. The kinematic analysis of the loop state equations provides the unknown geometric angles describing the loop in the *Austenite Free State*.

3.3.3.4. Kinetic Relations

Once the loop state angles are known the load at A can be determined using the geometric length constraint and the definition of C_4 (Equations 4 and 49) to be

$$P_{A} = \frac{16E_{A}IC_{4}^{2}}{L^{2}} \tag{50}$$

acting at an angle γ to the X axis. The load, P_A , is the internal force at point A that maintains the loop shape. The initial tension in the top of the loop, T_0 , can be determined using the equation of the tension in the top of the loop (Equation 7) and the initial Y component of the force P_A , P_{y0} , can be calculated using the relationship, $P_{y0} = P_A \sin(\gamma)$. While there are no external forces acting on the knit loop, internal tensions exist within the loop.

3.3.4. Austenite and Martensite Extended States

The development of the equations representing the Austenite and Martensite Extended States parallels that of the Austenite Free State. The force-equilibrium interactions are identical with friction still opposing extension. The governing differential equations for the Austenite Extended State are equivalent to those of the Austenite Free State, while the governing differential equations for the Martensite Extended State are the same except E_A (the Austenite elastic modulus) is replaced by E_M (the representative Martensite elastic modulus). However, with the kinematic relations an additional loop state equation is developed because the relationship between the wale width and course height must be determined as the textile is extended. The kinetic relations differ with the inclusion of an external load in the expression of the load P at the leg of the unit cell and the development of a load-deflection relation for both the unit cell and the entire textile. The kinetic and kinematic relations for the Austenite and Martensite Extended States are developed for Austenite as an illustration, where the Martensite relations differ only by the material modulus of elasticity E_M .

3.3.4.1. Kinematic Relations

The characteristic loop state angles must be calculated for the *Extended State* under applied loads as the textile extends, requiring an additional constraint because the wale width, W, narrows from the *Austenite Free State* as the course height, C, lengthens. The loop length, L, and the diameter, d, remain constant during extension therefore the wire diameter/loop length loop state equation (Equation 45) can still be used. The wale width/loop length loop state equation (Equation 43) establishes a relationship to the load dependent loop state angles (α , β , and γ). A third equation is necessary to solve for these unknown angles. This is derived from the assumption that the tension in the top of the loop, T, remains constant from the *Austenite Free State* as increases in the horizontal component of R are taken up through P due to symmetry thus there can be no change in horizontal loading [74] of the unit cell. Constant horizontal loop tension produces the relationship

$$T_{A} = \frac{-16E_{A}IC_{4}^{2}k_{1}}{L^{2}},$$
(51)

as derived from the equation for the tension in the top of the loop (Equation 7) and the equation for the load, P, applied at A (Equation 50). In the constraint for the tension at the top of the loop (Equation 51) the tension, T_A , is known from the *Austenite Free State*, and the loop length (L),

the moment of inertia (I), and the Elastic Modulus E_A are known values based on the phase of the material and the measured geometric properties, while C_4 and k_I are geometric functions of the unknown loop state angles. The set of three simultaneous transcendental algebraic equations for the extended state loop state (Equations 43, 45, and 51) can be solved to obtain the set of loop state angles that describe the loop shape for that extended state.

3.3.4.2. Kinetic Relations

The loops state angles are used to calculate the applied force and the corresponding deflection of the knit unit cell from the *Austenite Free State*. The kinetic behavior of the textile is calculated by scaling the force on the knit loop by the number of wales in the textile while the deflection is scaled by the number of courses.

The applied force distributed on each unit cell, F_{UC} , is the difference between the initial internal force component acting in the Y-direction, P_{y0} , and the Y-component of P, P_y , in the extended state and is calculated as

$$F_{UC} = P_{y} - P_{y0} \tag{52}$$

after using the kinetic equation (Equation 50) to determine the force, P, acting at A for the extended loop. The associated deflection is calculated using the geometric constraint between the course height and the wire diameter, the global Y-coordinate transformation, and the definition of C_2 (Equations 3, 28, and 47) as

$$\delta_{A,ext} = 2\left(\sqrt{\frac{E_A I}{P_A}}C_2 - \sqrt{\frac{E_A I}{P_A}}C_{20}\right) + d\left(\cos(\beta) - \cos(\beta_0)\right), \tag{53}$$

which represents the difference between the initial course height and the extended course height under known applied load. The force-deflection relationship is comprised of transcendental expressions for the applied loop force (F_{UC}) and the corresponding deflection ($\delta_{A,ext}$) which are parameterized by the wale width W. The set of loop state angles (α , β , and γ) obtained following the kinematic analysis are used in Equations 52 and 53 to compute the force and deflection relationship as the width of the wale decreases.

The model of the knitted textile is developed by scaling the force deflection model of the planar knit unit cell. It was assumed during the development of the knit model that a knit loop was made up of four identical unit cells rotated and reflected about the X and Y axes and a knitted textile was made of a matrix of knit loops. The total force in a knitted loop, F_{loop} , is twice that of the unit cell, $F_{loop}=2F_{UC}$, because there are two knit legs supporting the same force in each knit loop. The total force in a knitted textile is the addition of the force through all of the loops in the row or wale, N_W , and can be expressed as $F_{app}=N_WF_{loop}$. The extension of the unit cell is the same as the extension of a knitted loop therefore the extension of the textile is total extension through each course, N_C , and can be calculated using the relationship $\Delta=N_C\delta_{Aect}$. The load-extension of the knit unit cell is thus scaled to predict the load extension of the entire knitted textile.

3.3.5. Austenite Contracted State

The development of the equations for the Austenite Contracted State parallels that of the Austenite Free State. The force-equilibrium interactions are similar but sticking at the interlacing contact point (B) is assumed. The governing differential equations for the Austenite

Contracted State are exactly the same as the equations for the Austenite Free State. However, the kinematic relations require knowledge of the Martensite Extended State to enforce the assumption that no slipping occurs during actuation under a constant load, leading to two new loop state equations involving the applied load and constant segment length. The kinetic relations for the unit cell and the entire textile produce the load-extension relationship for the Austenite Contracted State while actuator displacement is provided by subtracting the Austenite Contracted State from the Martensite Extended State.

3.3.5.1. Kinematic Relations

During actuation the knit loops widen as the Martensite bending strain in the loop segments is recovered because the material stiffens during the transition into austenite. The interlacing contact point acts as a pin joint due to sticking between adjacent loops. The applied load in the Y-direction remains constant for the Austenite and Martensite Extended and the Austenite Contracted States since the actuation cycle occurs against a constant applied load,

$$F_{UC} = P_{yUC,Aext} = P_{yUC,Mext} = P_{yUC,Acont}$$
(54)

where $P_{yUC,Aext}$ is the load applied to extend the unit cell in the austenite phase, $P_{yUC,Mext}$ is the load applied to extend the unit cell in the martensite phase, and $P_{yUC,Acont}$ is the load under which the unit cell is actuated to the *Austenite Contracted State* from the *Martensite Extended State*. The actuation force, $P_{yUC,Acont}$, can be broken into two components,

$$P_{yUC,Acont} = P_{y,Acont} - P_{y0,Acont} = P_{Acont} \sin \gamma_{Acont} - P_{Acont0} \sin \gamma_{Acont0}. \tag{55}$$

Combining and rearranging the above equations in terms of known forces and angles gives

$$P_{Acont} \sin \gamma_{Acont} = P_{yUC,Mext} + P_{y0,Acont}, \tag{56}$$

where the applied load for the *Martensite Extended State*, $P_{yUC,Mext}$, and the *Y*-component of the *Austenite Contracted State*, $P_{y0,Acont}$, are known. The internal force acting on the knit unit cell at point **A**, P_{Acont} , can be calculated using Equation 50, resulting in

$$\frac{16E_A I C_4^2}{L^2} \sin \gamma_{Acont} = P_{yapp,Mext} + P_{y0,Acont}$$
(57)

which is a loop state equation for the new contracted loop geometry.

The geometric constraint that the segment lengths must add to a quarter of the measured loop length (Equation 4) is given by the same loop state equation as was used for the *Extended States*, (Equation 45), which is the second loop state equation for the *Austenite Contracted State*.

The third loop state equation is developed using the sticking assumption, which requires the lengths of segment AB and BC to remain constant during contraction. Since the previous constraint requires lengths to add to a quarter of the measured loop length only one segment (s_{AB} or s_{BC}) can be held constant without over-defining the system. Segment AB is held constant between the *Martensite Extended* and *Austenite Contracted* giving the relationship

$$\frac{s_{AB}}{L} = \frac{\hat{F}_{AB}}{4C_4} \tag{58}$$

Equations 45, 57, and 58 are the loop state equations for the *Austenite Contracted State* and are expressed in terms of measured geometric parameters previously determined from the *Martensite Extended* and *Austenite Free State*, and the unknown loop state angles. The set of three simultaneous algebraic transcendental equations can be solved numerically to determine the shape of the knit loop in the austenite contracted state.

3.3.5.2. Kinetic Relations

The actuation force is the same as the force applied to the unit cell, $P_{yUC,Acont}$ and is given by F_{UC} . The corresponding deflection from the *Austenite Free State* is provided by

$$\delta_{A,cont} = 2 \left(\sqrt{\frac{E_A I}{P_A}} C_2 - \sqrt{\frac{E_A I}{P_A}} C_{20} \right) + d \left(\cos \left(\beta \right) - \cos \left(\beta_0 \right) \right), \tag{59}$$

the same equation used for the *Austenite* and *Martensite Extended States*. The actuation displacement of the knit unit cell is the difference between the *Martensite Extended* and the *Austenite Contracted* deflections,

$$\delta_{act} = \delta_{M,ext} - \delta_{A,cont} \tag{60}$$

3.3.6. Textile Actuation Prediction

Prediction of the overall knit textile actuation from the unit cell model is done by scaling the force and actuation displacement of the unit cell in the *Austenite* and *Martensite Extended States* by the number of courses (rows) and wales (columns) in the textile. The total applied force under which the knit textile is actuating is $F_{app}=2N_WF_{UC}$, while the total actuator displacement of the knitted textile is $\Delta_{act}=N_C\delta_{act}$. The modeling procedure presented in this section produces an analytical model that captures the kinematic and kinetic behavior of each state experienced by this complex actuation architecture.

3.4. GARTER KNIT PATTERN EXPERIMENTAL VALIDATION

Experiments were conducted to understand the behavior of this new architectural actuation approach and assess the model's ability to predict the load-extension of each state and the net actuation. The model predictions were calculated in MATLAB using the measured initial geometric parameters of the knit prototype from the *Austenite Free State* (course height-C, wale width-W, wire diameter-d, and loop length-L) and material properties (E_A and E_M). The model prediction was compared to the experimental results for the load-extension curves in the *Austenite* and *Martensite Extended States*, the *Austenite Contracted State*, and also for net actuation between the *Martensite Extended State* and the *Austenite Contracted State*.

3.4.1. SMA Material Properties

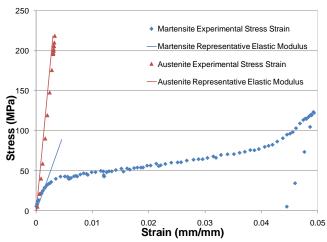


Figure 20. Experimental Material Properties of SMA Wire. The material properties are represented with linear elastic Austenite and Martensite Moduli.

The material properties of the Flexinol wire were experimentally determined before validation of the analytical model. The Austenite force-deflection curve for straight Flexinol 70°C wire was generated by electrically heating the straight wire above the material's Austenite finish temperature then measuring the load on the wire during axial elongation. Upon mechanical unloading, the wire returned to the Austenite free length and wire was cooled to 20°C (below the Martensite finish temperature). The Martensite force-deflection curve was generated by measuring the load on the wire during wire extension at this lower temperature. This process produced two stress-strain curves (Figure 20): a nearly linear austenite curve and a less stiff Martensite curve with a nearly constant stress plateau. Linear elastic approximations of

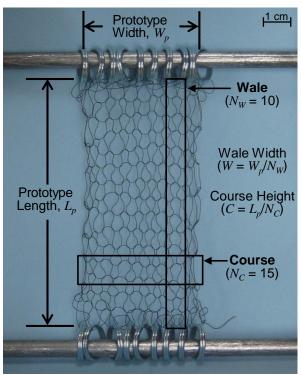


Figure 21. Garter Knit Pattern Active Knit Prototype. Picture of the garter knit pattern active knit prototype in the *Martensite Extended State* under a 1 N applied load labeled with prototype geometric parameters.

the stress-strain curves in the two phases were used, because the model assumes small strains during bending of the loops. The Austenite elastic modulus was found to be E_A =73 GPa while the representative Martensite modulus, taken from the initial low-strain slope, was E_M =19.8 GPa. These values are within the ranges of published elastic modulus values which vary from 70 to 75 GPa for Austenite and 18 to 28 GPa for Martensite [87]-[88].

3.4.2. Active Knit Prototype

A knit prototype was fabricated by hand knitting with 8 mil diameter, d, Dynalloy Flexinol 70°C shape memory alloy wire for 15 courses and 10 wales using 5.5 mm diameter knitting needles, D (Table 1, Figure 21). The reference length and width of the prototype in the *Austenite Free State* were measured to be L_{A0} =22.6 mm and $W_{totalA0}$ =85.0 mm. The average course height, C was determined by dividing the total prototype length by the total number of courses (N_C =15) resulting in a course height of 1.5 mm. Similarly, the wale width, W, was calculated by dividing the prototype width by the number of wales, (N_W =10), for a wale width of 8.5 mm. The total wire length in the knit prototype was determined post knitting by comparing the prototype weight to the weight of a single wire of known length with the same diameter, then the loop length, L, of a single knit loop was calculated by dividing the total length by the total number of loops in the prototype (N_C*N_W), resulting in a knit loop length of 20.2 mm.

3.4.3. Experimental Method

The prototype was mounted to the experimental setup in its *Martensite Free State* to parallel horizontal smooth rails at the top and bottom of the prototype which moved orthogonally on linear bearings along parallel guide rails that spanned the length of the prototype. Free lateral (wale-wise) contraction during longitudinal (course-wise) prototype extension was permitted by a series of steel rings attaching the knit actuator to the smooth rails. Free lateral motion is critical to maintain free boundary conditions and uniform deformations of all the loops within the prototype as assumed by the model.

The prototype was run through a thermo-mechanical cycle (Figure 16) in an Envirotronics EnviroFLX300 environmental chamber matching the same set of operational states and transitions upon which the model was based. The prototype was initially heated under no load to 100° C at which time the length of the prototype in the *Austenite Free State L*_{A0} (Figure 16a) was measured between the steel ring attachments using a US Digital linear encoder strip with 250 divisions per inch. The width of the entire prototype $W_{totalA0}$ was measured using digital calipers. A weight was attached to the prototype around a pulley, resulting in extension of the Austenitic prototype into the *Austenite Extended State* (Figure 16b) and the length L_{Aext} was recorded. The environmental chamber and the prototype were cooled to 20° C, the prototype continued to extend into the *Martensite Extended State* (Figure 16c), and length L_{Mext} was recorded. Heating the

Table 1. Garter Knit Pattern Prototype Geometric Parameters. Geometric parameters (d, D, N_C, N_W) used to create garter knit pattern knit and the measured Austenite Free State textile and unit cell geometries $(L_{A0}, W_{totalA0}, C_0, W_0, \text{ and } L)$.

| d (mil) | D (mm) | N_C | N_W | L _{A0} (mm) | $W_{totalA0}$ (mm) | | | L (mm) |
|---------|-----------|-------|-------|----------------------|--------------------|-----|-----|-----------|
| 8.0 | 5.5 | 15 | 10 | 22.6 | 85.0 | 1.5 | 8.5 | 20.2 |

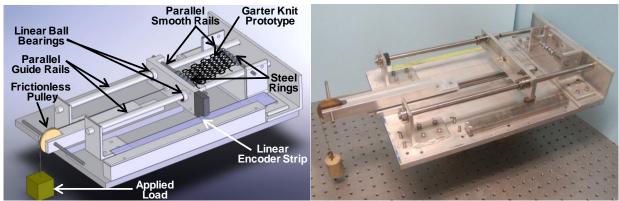


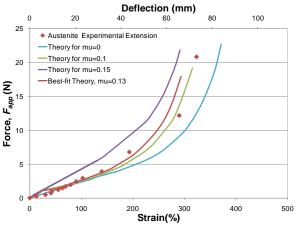
Figure 22. Experimental Setup. Experimental setup (schematic on left, experimental on right) used to determine the load-extension behavior of the Garter Knit Pattern States and the resulting actuation behavior.

environmental chamber and prototype to 100° C caused the prototype to contract under load into the *Austenite Contracted State* (Figure 16d), with a measured length of L_{Acont} . The weight was removed and the prototype returned to the *Austenite Free State* at which time a larger load was applied to the prototype and the testing process was repeated. This sequence ensures that the friction is acting against the elongation of the knit during extension and against contraction during actuation.

3.4.4. Austenite and Martensite Extended States

The experimental and theoretical results are shown in Figure 23 for Austenite Extended States and Figure 24 for the Martensite Extended States. Both the theory and experimental results of the Austenite and Martensite Extended States displayed "J" shaped load-extension curves similar to the load-extension curves of passive knits [73]-[74]. For each experimentally applied load (F_{app}) the knit prototype underwent a deflection from the Austenite Free State, Δ_{Aext} = L_{Aext} - L_{A0} for the Austenite Extended State deflection and Δ_{Mext} = L_{Mext} - L_{A0} for the Martensite Extended State deflection. During lower relative force loadings the knit underwent extreme stretching, up to approximately 200% strain for a 6 N applied load for the Austenite Extended State and 250% strain for a 3 N applied load for the Martensite Extended State. As the applied load was further increased the knit stiffened, the loops continued to stretch (up to 300% strain for the Austenite Extended State and 330% strain for the Martensite Extended State under an applied load of 15 N), but at a decreased rate because the loops experienced less change in curvature and more longitudinal alignment of the legs of the loop.

Using a friction value of μ =0.13, both the Austenite and Martensite theoretical load extension curves provided excellent correlation with the experimental data with an average relative displacement error of 6.1% and an average absolute displacement error of 1.9 mm over the experimental range of applied loads (0 to 20 N) for the *Austenite Extended State* and 4.1% average relative displacement error and 1.8 mm average absolute displacement error over the experimental range of applied loads (0 to 12 N) for the *Martensite Extended State*. The coefficient of friction (μ =0.13) was found independently for both the *Austenite Extended State* and the *Martensite Extended State* using a least squares analysis best fit over a range of coefficients between μ =0.1 and μ =0.15. The bounding coefficients of friction were chosen based on published values for the friction of smooth stainless steel materials [89]-[90]. A range of friction values were investigated because it is difficult to accurately measure the coefficient of friction between two wires. A coefficient of friction of μ =0.13 was independently found to be



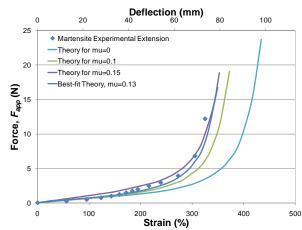


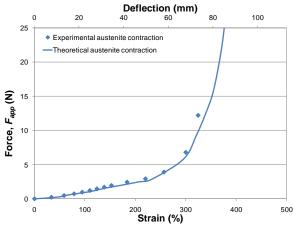
Figure 23. Austenite Extended State. Theoretical and Figure 24. Martensite Extended State. Theoretical experimental results agree with an average relative displacement error of 6.1% with coefficient of friction displacement error of 4.1% with coefficient of friction $\mu = 0.13$.

and experimental results agree with an average relative $\mu = 0.13$.

the best representation of the friction in each of the Austenite and Martensite Extended states, supporting the physical correctness of this parameter as opposed to a pure fit parameter. The theoretical load-extension results for the two friction cases bounded the majority of the experimental data points in both the Austenite and Martensite Extended States. The smaller friction value, μ =0.1, resulted in an average relative displacement errors of 10.4% for Austenite and 8.6% for Martensite over the range of applied loads for each state, while the larger friction value, μ =0.15, resulted in average relative displacement errors of 18.6% for Austenite and 7.5% for Martensite. All theoretical calculations involving friction provided vast improvements over the frictionless theory which was considerably less stiff than the experiments with an average relative displacement error of 22.3% for the Austenite Extended State and 22.5% for the Martensite Extended State over the range of applied loads for each state. While previous research has shown strong correlations between experimental and theoretical frictionless results (within 10% average displacement error [74], the inclusion of friction in the modeling of the load deflection of active knits vastly improved the average displacement error, reducing the error by 3.7 times for the Austenite Extended State and 5.5 times for the Martensite Extended case. Slippage between loops was observed during the operational transitions into the Austenite and Martensite Extended States, validating the friction assumptions used in the model.

3.4.5. Austenite Contracted State

The operational transition into the Austenite Contracted State from the Martensite Extended State included sticking of the interlacing contact point. The sticking of adjacent loops prohibited loops from sliding past one another, thus the actuation motion was solely a result of the loops straightening. The theoretical Austenite Contracted States were assembled to produce a loadextension relationship where the load is the applied force the knit actuates against (F_{app}) and the deflection (Δ_{Acont} = L_{Acont} - L_{A0}) is the difference between the recovered length and the length of the Austenite Free State. This theoretical load-extension relationship produces another "J" shaped curve which matches the experimental results in form and magnitude (Figure 25). Both the theoretical and experimental Austenite Contracted results are stiffer than that of the Martensite Extended load-extension curve, but less stiff than the Austenite Extended curve: the Austenite Contracted knit stretched under low force loadings to 220% strain for a 3 N applied load before



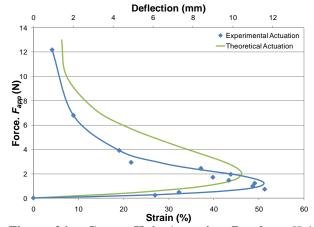


Figure 25. Austenite Contracted State. Theoretical **Figure 26.** and experimental results agree with an average relative displacement error of 2.8%. Prototype translation displacement error of 2.8%.

Figure 26. Garter Knit Actuation Results. Knit Prototype transitions between Martensite Extended and Austenite Contracted states to create theoretical actuation curve with same form as experimental results with an average absolute displacement error of 2.0 mm.

becoming stiffer as the knit stretched to 320% strain under a 15 N applied load. The loops were observed to stick during the operational transition into the *Austenite Contracted State*, validating the friction assumptions used in the model for this state. The theoretical *Austenite Contracted* curve quantitatively matches the experimental extremely closely with an average relative displacement error of 2.8% with an average absolute displacement error of 1.8 mm over the range of applied forces actuated against, 0 to 12 N.

3.4.6. Net Actuation

The net actuation performance ($\Delta_{ACT} = \Delta_{Mext} - \Delta_{Acont}$) is obtained by subtracting the displacement of the *Austenite Contracted State* from the *Martensite Extended State* at each applied load, as this is the motion obtained when actuating under a constant load. The theoretical and experimental actuation curves show the same distinctive qualitative performance (Figure 26). As the load increased the net actuation strain increased to a maximum peak actuator strain then decreased under increased applied loads as the prototype was not able to recover as much of the martensite strain. The shape of the actuation curves is unique: for small deflections, where the loops do not change shape much, net displacement increases as load increases since the performance is dominated primarily by the difference in stiffness between the two material phases. Whereas for larger deflections, where the loops are narrow and elongated, larger loads produce smaller net deflections since the austenite phase loses its ability to recover motion through the reduced leverage of the elongated loops. This implies that there is an optimal deflection point for designing such actuators to provide the maximum possible deflection (and a similar, but differently located configuration for maximum work) for which the predictive model can aid in designing the ideal active garter knit for a given application.

The theoretical and experimental actuation curves are also an excellent quantitative match given the complex behavioral form and assumptions made during the development of the analytical model. The peak actuator strain, 51.2%, was observed under a 1.22 N applied load while, theoretically, a 46.2% peak actuator strain was predicted under a 2 N applied load. The model accurately predicts the peak actuator motion within 5% strain at a higher applied force than experimentally witnessed. The experimental and theoretical actuation curves correlate with an average absolute displacement error of 2.0 mm over the 12 N range of applied actuation

forces which is slightly larger compared to 1.8 mm over each of the Martensite Extended and Austenite Contracted States. The differences between the theoretical and experimental actuation results stem from compounding the displacement errors for both the Martensite Extended and Austenite Contracted States through subtraction during the calculation of the actuation behavior and also result from the assumptions made during modeling, particularly, state dependent stickslip friction, full material transition into each state, and linear elastic material behavior. The friction assumption of constant sliding during extension gives larger strains than experimentally witnessed while the constant sticking assumption allows more force to be transferred under restricted motions consistent with the validation shown in Figure 26. The validity of the small strain assumption (and therefore the homogenous phase and linear elastic assumptions) can be estimated from the loop curvature by examining the ratio of the wire diameter, d, to the loop diameter as approximated by the knitting needle diameter, D. For the validation prototype, this ratio is 0.037, indicating that the largest strains, along the outer surface of the bent wire, violate the small strain assumption. However, in the Austenite Extended State the loops straighten significantly, reducing the maximum strain, and most of the material, even in the Martensite Extended State, will experience lower strains. Even with these assumptions the prediction was quite good, capturing the kinematic loop shape change and the kinetic performance of the contractile active knit.

Large actuation motions with unprecedented strains were observed during all the experiments. The garter knit pattern architecture significantly amplified the strain of a bulk individual fiber (in the case of SMA 8% recoverable and 3-4% actuation), to as much as 250% recoverable strain allowed for moderate forces of tens of Newtons and 51% actuation strain (Figure 26) under a 1.2 N applied load. The knitted actuator also provides enhanced force performance, axially contracting SMA wires 8 mil in diameter operate at a maximum strain of 4% under a 5.8 N applied load while the active knit prototype generated 4.1% strain under a large applied load of 12.2 N. The active knit actuator enhanced the strain by an order of magnitude and the force by two times that of the same diameter straight SMA wires, affording enhanced actuation capabilities to a variety of application domains and enable new technologies.

3.5. Two-Dimensional Analytical Model Conclusions

This section expanded upon existing knit models to capture the cyclic actuation behavior of planar active knits by incorporating the dual states of the material and the various friction states between interlacing adjacent loops. The active knit predictive model was developed by defining the operational states, identifying and geometrically defining the smallest repetitive unit cell, developing predictive capabilities of the active knit loop and garter knit pattern active textiles, and experimentally validating the model.

The first step in developing the active knitted loop model was to outline the typical actuation cycle of garter knit pattern textiles: *Austenite Free*, *Austenite Extended*, *Martensite Extended*, and *Martensite Contracted States* while considering the mechanical and thermal operational transitions the textile undergoes during deformation. While the first level of the hierarchy is the knitted loop, the smallest repetitive element, or unit cell, is a quarter of a knit loop. Geometric constraints are developed and force equilibrium analysis of the unit cell is completed while assuming different friction conditions (stick or slip) during the operational transition depending on the loading and the initial state of the textile. Elastica Theory and Euler Bernoulli beam bending are used in addition to the knit geometry and the force equilibrium to develop governing

differential equations that can be solved to determine the deflection from the Austenite Free State of the textile and thus the relative displacement between the Martensite Extended and Austenite Contracted States for constant load actuation. A set of fully analytical transcendental algebraic equations (as opposed to a set of coupled differential equations) describe the deflections experienced within a unit cell for each operational state, and are scaled to produce the load-extension properties of the entire garter knit pattern textile for each state as well as the net actuation performance.

The analytical model of the knit loop and garter knit pattern was experimentally validated for its ability to predict the load extension behavior of each of the states and the constant load actuation performance. A garter knit pattern prototype was fabricated from 70°C Flexinol® wire with a diameter of 8 mil using 5.5 mm knitting needles for 10 loops and 15 rows. The prototype was cycled through the modeled sequence of operational states under a variety of external loads from 0 to 12 N in order to validate the model. The model predicts the load extension behavior of the textile in each of the states in addition to predicting the load extension actuation performance, providing an excellent match to the experimental results particularly considering the modeling assumptions: dual stiffness, linear-elastic material with prescribed friction states. The Martensite and Austenite Extended States were predicted with an average relative displacement error of 4.1% and 6.1% using a coefficient of friction μ =0.13 as found independently via a best fit analysis for each the Martensite and Austenite Extended States. The theoretical Austenite Contracted State agreed with the experimental results with a 2.8% average relative displacement error. The results validate the observed friction requirements - sliding for Extended States and sticking for Contracted States. The theoretical actuation, the difference between the Martensite Extended and Austenite Contracted States, was found to match the form and magnitude of the experimental results with an average absolute displacement error of 2.0 mm. The model accurately predicts the qualitative and quantitative performance of planar contractile garter knit pattern active knits.

The unique shape of the actuation curve with increasing net displacement versus force at low load, a maximum displacement peak, and decreasing displacement at further increasing loads provides the opportunity for tailoring of architectural parameters such as loop size, wire diameter, and the number of courses and wales within the textile to optimally match the specific needs of a particular application. This highly leveraged garter knit pattern architecture allows for large strains (51%) at moderate forces (1.22 N) and usable strains (4.1%) at enhanced forces (12 N) over the material alone (4% strain at 5.8 N). This new actuation capability goes beyond what is possible with conventional actuation technology and the current state of the art in smart materials actuators, meeting increasing needs for large contractile actuation surfaces.

The development of the two-dimensional analytical active knitted loop model provides the capability to predict the large strain, moderate force kinetic performance of planar active knits, which is a capability that did not previously exist. The incorporation of friction between interlacing adjacent knitted loops in the active knitted loop model greatly improved the average displacement error by reducing the error by 3.7 times for the Austenite Extended State and 5.5 times for the Martensite Extended case. Additionally, the inclusion of the dual state, multistiffness material enabled the model to capture the cyclic actuation behavior. The inclusion of friction and the dual state material was required to capture the hysteretic behavior of active knitted structures, producing an analytical model that provides a tractable tool for the prediction, design, and tailoring of active garter knit pattern actuators. In addition, the model provides an

improved ability to predict the kinetic performance of all knitted loops (active and passive) with higher fidelity than previously possible and an analytical form that is better suited for design. Both active and passive knits experience friction between adjacent loops, therefore the inclusion of friction in a knit loop model can increase the accuracy provided by the model to better represent the kinetic performance of all knit loops. The inclusion of friction also enables the analysis of passive knits that undergo multiple operating states including cyclic loading and thermal loading during manufacturing. The developed model is useful for predicting the kinetic actuation performance of planar knits and provides a framework for developing a three dimensional model that can capture the out of plane behavior of more complicated knit patterns.

4. FEASIBILITY DEMONSTRATION – FLOW CONTROL CASE STUDY

Active knits are a promising actuation architecture that produces unique actuation motions which are unattainable with current technologies, however, the feasibility of using active knits in applications has yet to be demonstrated. This section presents a feasibility demonstration study for using rib knit pattern active knits to meet the performance specifications required for flow control of an aircraft.

Flow control has been of significant interest to the aerospace community because actively manipulating flow characteristics around the wing can enhance high-lift capability and reduce drag by delaying or preventing boundary layer separation; thereby, increasing fuel economy and improving maneuverability and operation over diverse flight conditions which enables longer, more varied missions [1]-[2]. It is predicted that increasing flight efficiency would result in a one percent saving in world consumption of jet fuel worth approximately \$1.25 million a day of direct operating costs [91]. Likewise, such fuel savings would lead to reduced environmental impact such as reduced noise and carbon emissions. Engineers have tried numerous tools (wing flaps, spoilers, vortex generators, etc.) to change the effective shape of the wing mid-flight to provide flow control. The simplification of conventional high lift systems by flow control technologies could possibly lead to a 0.3% airplane cost reduction, up to 2% weight reduction and about 3% cruise drag reduction [92]. While wing flaps, spoilers, and vortex generators have provided improvements at the leading and trailing edge of the wing, their large size and weight have prohibited full integration of actuators distributed over the wing surface.

One method that has produced incremental improvement to active flow control using distributed actuation is synthetic jets. Synthetic jets are used to create puffs of air at high frequencies to introduce a nearly constant controlled boundary layer disturbance that prevents or delays separation of the boundary layer across the wing, reducing the wake over the wing and improving efficiency [93]-[96]. Traditional synthetic jets implemented using pneumatics and electromagnetics are robust and provide the necessary airflow but their added design complexity and the increased manufacturing and operating costs of the system has constrained their use [93]-[96]. While piezoelectric jets offer a more compact and lightweight solution, current approaches exhibit failure of the diaphragm due to debonding and cracking at the high operating frequencies, restricting their adoption on aircraft [94]-[96].

A second approach to flow control is to vary wing surface conditions, via small/medium scale distributed actuation, to minimize drag and maximize efficiency while maintaining a continuous, smooth, aerodynamic structure. Surface contour bumps, a local change in the shape of the wing, have been computationally shown to reduce drag by 15% under transonic flow conditions [97]. Experimentally replicating the improved flow characteristics of contour bumps is difficult because varying the bump height and creating larger gradual bump surfaces pose technical difficulties [97]. Shape modification can also be accomplished using surface texturing to create small dimples that can produce vortices of prescribed strength and duration for the real time control of aerodynamic flows [98]-[99]. Generally, aircraft fly in turbulent flow regimes with 50% of cruise drag arising from skin friction [100]. A layer of harmonically forced dimples can be used to generate span-wise travelling vortices that are known to reduce turbulent skin friction drag by as much as 30% [98]-[99]. Another form of flow control can come from ribs dispersed over a wing surface to reduce shear stress on the wings by obstructing span-wise

movement of the fluid. Optimal rib shape and arrangement can lead to shear stress reductions of 9.9% [97].

Flow control approaches using local surface shape changes have shown significant theoretical improvements to flight efficiency under specific off-design flight conditions, however, the actuator technology needed to realize flow control approaches does not currently exist. Large transonic aircraft fly up to a ceiling height (maximum altitude) of 10 to 20 km in the compressible flow regime. Using basic compressible flow equations and published pressure coefficients across the wing, the pressures on aircraft wings can be determined [101]. The average free-stream pressures range from approximately 10 to 16.5 kPa at the ceiling altitudes, e.g. F-22 Raptor at a ceiling altitude of 9.8 km experiences pressures of 10.1 kPa [102]. At these high pressures surface displacements ranging from 10 to 30 mm are required for successful flow control applications such as surface bumps and ribs. The flow control approaches need to be actively actuated mid-flight as not to disrupt the flow over the wing during normal flight conditions for which the original wing has been designed. In order to achieve this in-flight surface change, actuators that are capable of large three-dimensionally complex distributed motions and that can be embedded in the wing must be developed.

This section provides the result of a feasibility demonstration study that investigates the potential of using an active rib knit pattern actuators to create contour bumps for flow control. The orientation and configuration of rib knit pattern textiles are described. A rib knit pattern active knit prototype is created and tested using a specially designed experimental rig. Series and parallel combinations of identical rib knit pattern prototypes are experimentally explored to meet the technical specification required by the contour bump application. The measured knit performance is on the scale of the necessary aerodynamic pressures and displacements; thus, the rib knit pattern active knit is promising as a technical solution for distributed actuation of local surface profiles in flow control. This feasibility demonstration study shows that active knit pattern textiles can be used in applications by exploiting their unique performances to meet the kinematic and kinetic specifications new applications.

4.1. RIB KNIT PATTERN ARCHITECTURE, OPERATION, AND CONFIGURATIONS

Rib knit pattern knits leverage the active base material capability to create large strains distributed over a surface through the utilization of a unique rib knit pattern architecture, multistate operation, and structural architectural configurations.

4.1.1. Architecture

All knit architectures are created using two types of loops – knit loops and purl loops. Both types of loops are characterized by a unit cell containing a loop, ridge, and two legs (Figure 27a). The tear drop shaped upper portion of the unit cell is the loop, which extends providing the legs which attach unit cells to one another. The ridge is the uppermost portion of the loop from the previous course (row of loops), which intersects with the loop and divides the loop from the legs. Knit and purl loops are differentiated by the location of the ridge relative to the loops and legs. Knit loops have backward arching loops with ridges in the back. The legs of the knit loop interlock with the ridge then extend behind the ridge, maintaining the curvature of the loop. The purl loop is the opposite of the knit loop with a forward arching loop with forward ridges and legs that extend to the front. A knit loop on one side of a textile appears as a purl loop on the

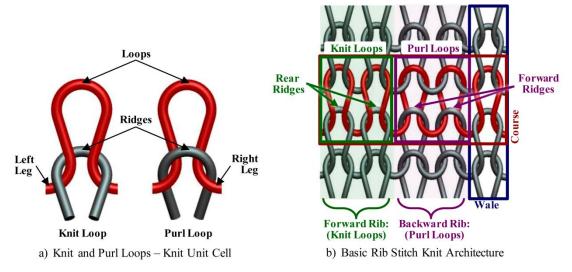


Figure 27. Knit Architecture. Knit textiles are comprised of two basic unit cells, knit and purl, which can be combined to form different architectural stitches. The rib stitch architecture is comprised of two knit loops alternating with two purl loops forming symmetric columns.

other. Different combinations of the two basic loop structures enable myriad architectures to be created.

The combination of knit and purl loops of particular interest for flow control applications is the rib knit pattern architecture (Figure 27b). The rib knit pattern is created by alternating knit and purl loops across the first course, or row. After the first course is completed, knit loops are purled and purled loops are knit in each additional course. The alternation of the fundamental unit cell produces symmetric wales (columns), alternating between smooth columns of the forward ribs comprised of knit loops and columns of ridges formed by the backward ribs comprised of purl loops. The rib knit pattern architecture can be fabricated by alternating a single knit and a single purl loop, called a 1x1 rib, or by alternating combinations of multiple knit and purl loops. The most common rib knit pattern architecture is a 2x2 rib which alternates two adjacent knit loops with two purl loops, creating raised and depressed columns that are two loops wide as shown in Figure 27b.

4.1.2. Operation

SMA rib knit pattern knit textiles go through operational transitions from one state to another resulting in a change in height and stiffness of the textile as depicted in Figure 28. The textile is initially compressed by an applied load (F_{app}) to the Martensite Compressed height (h_{Mcomp}), while the material is in the less stiff Martensite phase. An operational transition occurs when the material is heated above the transition temperature (T_{Af}) into the Austenite phase causing the textile to lift the applied load to the Austenite Expanded height (h_{Aexp}). A second operational transition returns the textile to the Martensite Compressed height (h_{Mcomp}) upon cooling below the Martensite Finish temperature (T_{Mf}), completing the typical actuation cycle (Figure 28) which cycles between the Martensite Compressed State and the Austenite Expanded State

4.1.2.1. Martensite Compressed State

The first state, the Martensite Compressed State, is reached when a compressive load, F_{app} , is applied to the textile in the cooled, less stiff state at a temperature below the Martensite Finish

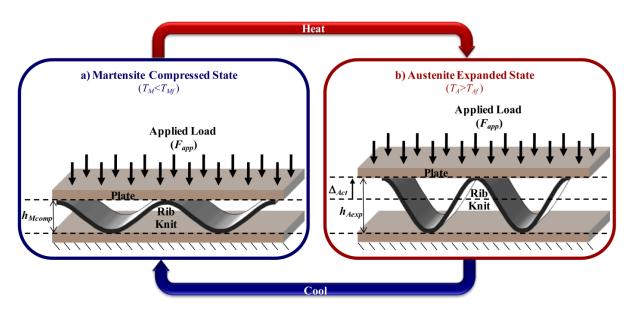


Figure 28. Rib Stitch Operation. The rib stitch distributed actuator cycles between the Martensite Compressed State and the Austenite Expanded State under a constant applied load (F_{app}) via a thermal operational transition between the low temperature Martensite phase (T_M) and the high temperature Austenite phase (T_A) .

temperature (T_{Mf}) , compressing the textile to the Martensite Compressed height, h_{Mcomp} (Figure 28a). The textile compresses under the applied load as the contact areas at the peaks and valleys of the textile slip horizontally and the forward ribs at the peaks are pushed down while the backward ribs at the valleys are pushed up. The applied load normal to the plane of the knit applies off-set forces in the normal direction between adjacent courses at the interaction points that result in force couples at each interaction point in the knit structure. Figure 29 shows two different sets of force couples: the first set is a pair of balanced force couples at the top of a knit loop in the forward rib column that create moments of equal magnitude that balance in different directions (one clockwise the other counterclockwise). The second set is a pair of unbalanced force couples at the bottom of a loop that connects a knit loop to a purl loop that creates two moments of equal magnitude in the same direction. The legs connecting forward ribs to backward ribs connect knit and purl loops on either side and have a clockwise moment applied to each constrained end (Figure 29). The bending loading on the leg encourages the compression of the textile because the compliant Martensite material bends to horizontally flatten the leg, compressing to the Martensite Compressed height, h_{Mcomp} . The Martensite Compressed State is the first of two states in the quasi-static cyclic portion of the typical actuation cycle.

4.1.2.2. Austenite Expanded State

The second state in the actuation cycle, shown in the rib knit pattern operation figure (Figure 28b), is reached when the textile is heated under the same applied load, F_{app} , to above the Austenite Finish transition temperature (T_{Af}), recovering the plastic deformations experienced in the Martensite state to become stiffer through utilization of the Shape Memory Effect of the foundational SMA wire. The rib knit pattern textile is comprised of bent loops of SMA wire which is trained to a straight shape by the manufacturer. Upon heating, the loops attempt to return to their naturally straight configuration, increasing the width of individual loops while decreasing the loop height. The structural force couples between interacting adjacent courses, described in the previous section, are still present in the actuated structure. The combination of the increased stiffness of the material and the unbalanced force couples cause the legs at the

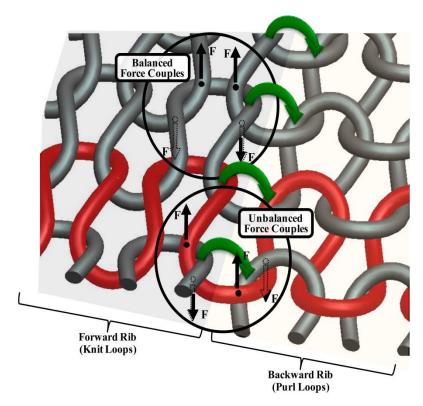


Figure 29. Rib Stitch Actuation Mechanism. The unique accordion actuation behavior of the rib stitch architecture is a result of the unbalanced force couples in each course between forward and backward ribs that lifts columns of forward ribs upward while depressing columns of backward ribs downward.

bottom of the loop connecting forward ribs and backward ribs to lift the forward ribs while depressing the backward ribs, raising the prototype to the Austenite Expanded height (h_{Aexp}).

4.1.3. Rib Knit pattern Architectural Configurations

The rib knit pattern architecture is extremely versatile, and numerous combinations of loops can be used to slightly modify the knit pattern architecture. Performance enhancing modifications can be made by creating architectural configurations using multiple individual rib knit pattern textiles such as stacking (series) and nestling (parallel).

4.1.3.1. Stacking

Stacking is an architectural configuration obtained by placing multiple individual rib knit pattern textiles on top of each other, where each textile is separated by a thin, rigid plate (**Figure 30**a shows two stacked textiles). The individual rib knit pattern textiles work in series, the applied load is transferred through each individual textile while each textile is free to expand or compress in response to a thermal operational transition. The stacked architecture maintains the original height of each individual textile while scaling the total height by the number of stacked textiles in the actuator. The stacked architectural configuration results in a final actuator with the same footprint and a scaled volume compared to an individual actuator that produces scaled displacement under the same applied load.

4.1.3.2. **Nestling**

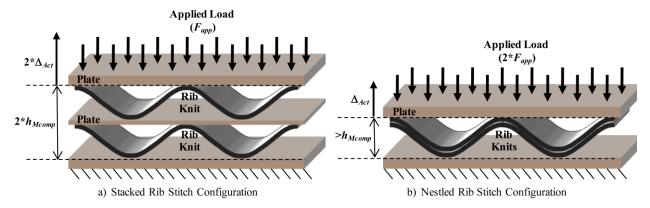


Figure 30. Architectural Configurations. Stacked rib stitch configuration, two identical individual rib stitch prototypes separated by a thin rigid plate, provides additive displacement (acts in series). Nestled rib stitch configuration, two identical rib stitch prototypes placed directly on top of each other while matching the peaks and valleys, provides additive force (acts in parallel).

The second architectural configuration, nestling, requires the entire top surface of one rib knit pattern textile to contact the bottom surface of another rib knit pattern textile (two nestled textiles are shown in Figure 30b). The textiles are placed on top of each other such that the forward and backward rib columns of each of the textiles are aligned. The nestled rib knit pattern textiles work in parallel, each textile undergoes the same displacement throughout the actuation cycle while supporting twice the load as each individual textile supports the same load. Nestling doubles the thickness of the textile, resulting in an actuator with a slightly larger height while maintaining the footprint of the actuator.

4.2. RIB KNIT PATTERN EXPERIMENTAL EVALUATION

An experimental evaluation was conducted to quantitatively compare the performance capability of the rib knit pattern architecture and architectural configurations to the local surface modification specifications for flow control applications. The flow control applications of interest require areas of the surface of the wing to be elevated above the fixed wing shape to create bumps between 10 and 30 mms in height acting against aerodynamic pressures in the range of 10 to 16.5 kPa. To assess the ability for the active rib knit pattern knit to meet this realm of operation, experiments were conducted to characterize the quasi-static force-displacement performance of the four forms of the rib knit pattern configurations: individual, stack, nestled and stack-nestled.

4.2.1. Rib Knit pattern Prototype Fabrication

Individual rib knit pattern knit prototypes (textiles) were fabricated by hand knitting 20 mil Dynalloy Flexinol 70°C shape memory alloy wire with 6 mm traditional knitting needles for 14 courses (rows) and 16 wales (columns) using a 2x2 rib knit pattern architecture (Table 2, Figure 31). The first course of the 2x2 rib knit pattern architecture was created by casting on a single knit loop, alternating two purl loops and two knit loops, and ending with a single knit loop. In each subsequent course, knit loops were purled and purl loops were knit to create the final knit pattern. The textiles contained 7 complete ribs that occupied 2 wales, and two single wale ribs on either side of the textiles. All ribs extended through all 14 courses. Four individual rib knit pattern textiles were made, each weighed 19.6 g and measured 140.0 mm in width by 72.1 mm in length for a surface area of 0.010 mm². The four textiles were combined to make five rib knit

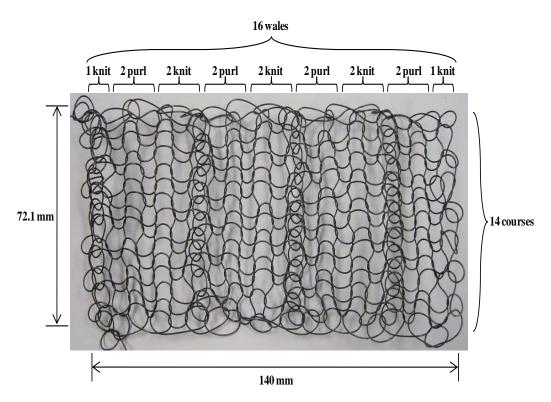


Figure 31. Rib Stitch Knit Prototype. Rib stitch knit textile knit with 20 mil Flexinol 70°C wire on 6 mm knitting needles for 14 courses and 16 wales in a 2x2 rib stitch pattern.

pattern architectural prototypes to be independently experimentally tested: two individual rib knit pattern prototypes, two individual textiles for a stacked prototype, two individual textiles for a nestled prototype, and four individual textiles for two nestled textiles stacked on top of each other to create a stacked-nestled prototype.

4.2.2. Experimental Setup and Procedure

To determine the expansive distributed surface actuation performance of the rib knit pattern architecture, the following setup and procedure (Figure 32) was used to measure the actuation height in response to an applied constant load. Each prototype in its Martensite state was placed on a smooth aluminum base plate and heated until fully actuated in austenite state under no load using a Milwaukee Digital Heat Gun Model 3300 to ensure proper phase transition upon cooling. Another smooth aluminum plate, the slider plate, was placed on top of the rib knit pattern prototype, compressing it slightly. The slider plate moved vertically (parallel to the base plate) on linear bearings along four orthogonally aligned parallel precision ground stainless steel guide rails. The prototype was run through thermo-mechanical cycles (Figure 28) in an Envirotronics EnviroFLX 300 environmental chamber. The environmental chamber and the prototype were

Table 2. Rib Stitch Prototype Parameters. Material (transition temperature), Geometric (wire diameter, needle diameter, number of course and wales) and Architectural (rib pattern) parameters used in rib stitch knitted prototypes fabrication and the resulting physical measurements of the knits (width, length, area, and mass).

| Wire diameter (mil) | Transition Temperature | Needle Diameter (mm) | Number Courses | Number Wales | Rib Pattern | Width (mm) | Length (mm) | Area (mm²) | Mass (g) |
|---------------------------|---------------------------|----------------------------|-------------------|-----------------|----------------|---------------|-------------|------------------|----------|
| (11111) | (C) | (111111) | | | | (111111) | (111111) | (IIIIII <i>)</i> | (g) |

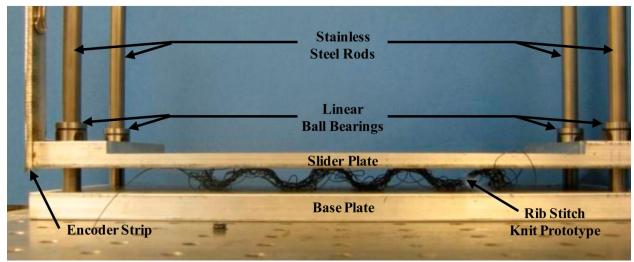


Figure 32. Experimental Setup for Testing of Rib Stitch Knitted Prototypes. The rib stitch prototype expands from the Martensite Compressed State to the Austenite Expanded State to lift the slider plate and any additional applied loads.

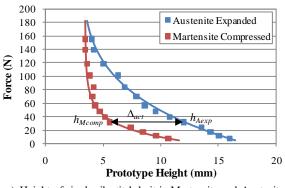
cooled to 10° C and the initial Martensite compressed height was measured using a US Digital linear encoder strip with 500 divisions per inch. A weight was applied to the top of the top aluminum plate, compressing the prototype. The environmental chamber and the prototype were heated to 100° C causing the material to transition into the Austenite phase and the prototype to expand into raised rows of arches (Figure 28b), characteristic of the Austenite Expanded State, with a recorded height, h_{Aexp} . The temperature was reduced to 10° C, the prototype compressed in response to the material transition into the Martensite phase, and the sample returned to the Martensite Compressed State with a height of h_{Mcomp} (Figure 28a) Additional weight was applied to the prototype and the thermo-mechanical testing cycle was repeated to obtain a force deflection performance curve.

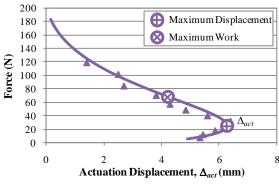
4.2.3. Experimental Results

Each of the rib knit pattern prototypes and the architectural configurations display the same operational states and form (Figure 28). The initially compressed nearly planar prototype expands vertically by creating a series of raised and lowered semi-cylindrical ridges as the temperature increases above the austenite finish temperature. Upon cooling, the prototype compresses, completing the actuation cycle. Every prototype produced very large displacements under significant applied loads. As the applied load increased the net actuation increased to a maximum then decreased under increased applied loads.

4.2.3.1. Single Rib Knit Pattern Prototypes

Two single rib knit pattern knit prototypes were experimentally tested individually. The first individual prototype was actuated against an applied load of 24.7 N (approximately equivalent to 2.5 kPa calculated as a distributed pressure over the footprint of the prototype in the Martensite Compressed State) to the Austenite Expanded height (h_{Aexp}) of 13.1 mm (red curve in Figure 33a). The material was cooled to the Martensite phase causing the prototype to compress under the applied load to the Martensite Compressed height (h_{Mcomp}) of 6.8 mm (blue curve in Figure 33a). The 6.3 mm net actuation motion of the individual rib knit pattern prototype, Δ_{act} , was calculated as the difference between the actuated height of the Austenite Expanded State and the compressed height of the Martensite Compressed State (Δ_{act} = h_{Aexp} -





a) Height of single rib stitch knit in Martensite and Austenite

b) Actuation performance of single rib stitch knit

Figure 33. Single Rib Stitch Knit Prototype. The Austenite Expanded and Martensite Compressed states for a single rib stitch knit prototype (knit with 20 mil Flexinol 70°C wire on 6 mm knitting needles for 14 courses and 16 wales in a 2x2 rib stitch pattern) over a range of applied loads are show, the actuation displacement is the change in height between the two states.

 h_{Mcomp}) and plotted against the constant applied load in Figure 33b. This process was repeated for a range of applied loads, producing an actuation curve (Figure 33b) characteristic of knitted actuators [103] that provides increasing net actuation under increasing applied loads to a maximum peak actuator displacement (peak marked with a cross in Figure 33b) then decreased net actuation under further increased applied loads. The initial increase in actuation displacement under increased applied loads is a result of the larger applied loads greatly decreasing the height of the prototype in the Martensite Compressed State, which is recovered upon actuation to the Austenite Expanded State. As larger loads are applied, the height of the prototype in the Martensite Compressed State continues to decrease but the material is no longer able to recover the strain when actuated into the Austenite Expanded State, resulting in smaller net actuation displacement for increased applied loads. This actuation behavior implies that there is an optimal point for designing actuators to provide the maximum deflection possible. The first individual prototype provided a maximum displacement of 6.3 mm under a 2.5 kPa applied load, highlighted with the cross in Figure 33b. Likewise, there is a similar point on the actuation curve at a larger applied load which provides the maximum work, 286.2 Nmm, producing 4.2 mm of displacement under a 6.7 kPa applied load, highlighted with an \otimes in Figure 33b.

The experimental process was repeated for the second individual rib knit pattern prototype, revealing that the actuation performances of the two individual prototypes (green and purple curves in Figure 34) were kinetically very similar with an average displacement error of 7.7% over the range of applied loads, inferring small inconsistencies in the hand knit prototypes have little influence on the mechanical behavior of the actuator. The second individual rib knit pattern prototype produced a net actuation displacement of 6.4 mm under an applied load of 13.7 N (Figure 34), which is equivalent to a pressure of 1.4 kPa, calculated as a distributed pressure over the entire footprint of the prototype in the Martensite Compressed State. The maximum work, 263.5 Nmm, occurred under an enhanced pressure, 8.1 kPa, due to the unique load-displacement performance. As the individual samples were knit using identical geometric and architectural parameters, they each weighed 19.6 g and had a surface area of 0.010 m², providing very close maximums for specific work (29.2 J/kg and 26.9 J/kg) and work density (7.1 kJ/m³ and 5.9 kJ/m³) at the same applied load as the maximum work performance point. The individual prototypes produce displacements and pressures in the same order of magnitude as required for

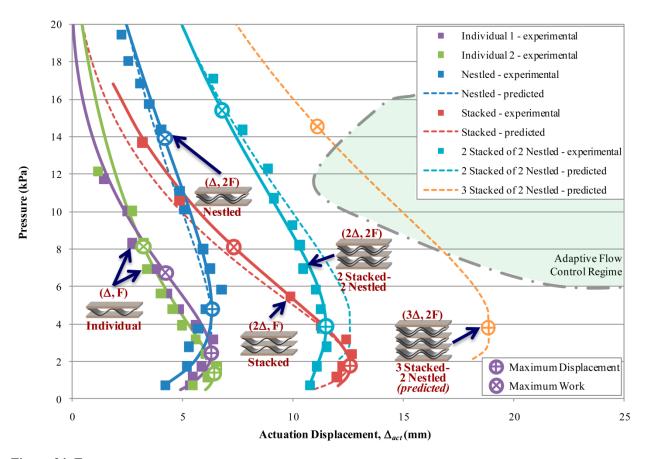


Figure 34. Experimental and Predicted Results for Rib Stitch Knitted Actuators. Rib stitch knitted prototypes (knit with 20 mil Flexinol 70°C wire on 6 mm knitting needles for 14 courses and 16 wales in a 2x2 rib stitch pattern) were combined by stacking and nestling to provide enhanced displacements and forces that approach the application specification region for flow control applications.

flow control applications and can be used as a building block to produce the required displacements under aerodynamic loads.

4.2.3.2. Stacked Rib Knit Pattern Prototype

Stacking of two individual rib knit pattern textiles was investigated to increase the actuation displacement of the rib knit pattern actuator. The two individual rib knit pattern portions were separated by a thin rigid aluminum plate and work in series. The applied load was transferred through each individual textile while each textile was free to expand and/or compress against the applied load. The experimental behavior of the stacked prototype (shown with red squares with a solid red line in Figure 34) closely matches the predicted behavior obtained by adding the displacements of the individual prototypes for an applied load (shown with red dashed line in Figure 34) with an average displacement error of 5.5% over the range of applied loads. This confirms the additive displacement series behavior of the stacked architectural configuration. The experiments verified this behavior with twice the maximum actuation displacement (12.6 mm for stacked compared to 12.5 mm for the additive displacements of the individuals) under the same applied load (stacked actuated under 17.7 N or 1.8 kPa while the predicted applied load under max displacement was 19.2 N or 1.9 kPa). The maximum work was also increased by stacking the individual textiles: more than twice the maximum work (595.9 Nmm) was produced compared to a single rib knit pattern knit architecture (286.2 Nmm and 263.5 Nmm) as the

Table 3. Rib Stitch Experimental Results. Experimental results of Individual, Stacked, Nestled, and Stacked-Nestled Rib Stitch

Prototypes comparing performance at maximum displacement and maximum work operating points.

| Prototype | | | | Pressure @ Max Disp (kPa) | | | | Disp @ Max Work (mm) | Max Specific Work (J/kg) | Max Work Density (kJ/m³) |
|------------------------|------|------|------|---------------------------------|--------|------|------|----------------------------|--------------------------------|--------------------------------|
| Individual 1 | 6.3 | 91.7 | 24.7 | 2.5 | 286.2 | 6.7 | 4.0 | 4.2 | 29.2 | 7.1 |
| Individual 2 | 6.4 | 80.7 | 13.7 | 1.4 | 263.5 | 8.1 | 4.4 | 3.2 | 26.9 | 5.9 |
| Stacked | 12.6 | 86.5 | 17.7 | 1.8 | 595.9 | 8.1 | 7.7 | 7.3 | 30.4 | 7.7 |
| Nestled | 6.3 | 61.5 | 48.4 | 4.8 | 586.7 | 13.9 | 5.1 | 4.2 | 29.9 | 11.4 |
| Stacked and Nestled | 11.5 | 64.5 | 39.0 | 3.9 | 1053.9 | 15.4 | 11.1 | 6.8 | 36.2 | 9.4 |

displacement corresponding to the maximum work was increased from 4.2 mm and 3.2 mm of the individual prototypes to 7.3 mm for the stacked actuator. The enhanced maximum work corresponds to similar maximum specific work (30.4 J/kg for stacked compared to 29.2 J/kg and 26.9 J/kg for individuals) and work density (7.7 kJ/m³ for stacked compared to 7.1 kJ/m³ and 5.9 kJ/m³ for individuals) as both the mass and volume of the prototype doubled while producing twice the actuation displacements. The stacked architectural configuration doubles the actuation displacement, resulting in useable displacements to adequately change the shape of the wing to improve flow control.

4.2.3.3. Nestled Rib Knit pattern Knit Prototype

Two rib knit pattern textiles were nestled, placed directly on top of each other matching the peaks and valleys of the forward and backward ribs, to actuate against larger loads compared to individual prototypes. The nestled prototype acts as two individual textiles in parallel, for the same actuation displacement each individual rib knit pattern knit textile carries the same load as the individual experimental tests. The parallel additive force behavior of the nestled architecture is confirmed by the experimental behavior of the nestled prototype (shown with blue squares in Figure 34) matching the added forces of two individual textiles under the same displacement (shown with the dashed blue line in Figure 34) with an average displacement error of 5.0%. The nestled architectural configuration more than doubles the load (48.4 N or 4.8 kPa for the nestled configuration compared to 24.7 N or 2.5 kPa and 13.7 N or 1.4 kPa for individuals) under which the prototype provides the same max displacement (6.3 mm for nestled compared to 6.3 mm and 6.4 mm for the individual prototypes). The enhanced stiffness of the nestled actuator provides twice the work (586.7 Nmm) as the single rib knit pattern knit actuators (286.2 Nmm and 263.5 Nmm) at double the aerodynamic load (13.9 kPa for the nestled compared to 6.7 kPa and 8.1 kPa for the individuals) while providing the nearly the same actuation displacement (4.2 mm for nestled compared to 4.2 mm and 3.2 mm for individuals). The nestled architecture provides essentially the same maximum specific work (29.6 J/kg compared to 29.24 J/kg and 26.9 4 J/kg for individuals) because the force and total mass have doubled. The nestled architectural combination doubles the work density (13.0 kJ/m³ compared to 7.1 kJ/m³ and 5.9 kJ/m³ for individuals) since twice the work was done in nearly the same package size. Nestling two individual samples increases the pressure at which the actuator can do usable work, actuating against aerodynamic level loads.

4.2.3.4. Stacked-Nestled Rib Knit pattern Knit Prototype

These experiments confirm that stacking increases displacement additively and nestling increases force additively, with both in the realm of necessary to realize flow control applications. By combining the two types of rib knit pattern knit architectural configurations (stacking and nestling), the specifications for the displacement and loading for flow control can be reached. Four individual rib knit pattern knit textiles were arranged by stacking two sets of two nestled textiles on top of one another. The stacked-nestled prototype produces increased displacements under increased loading (shown with teal circles in Figure 34) that corresponds to an average displacement error of 5.8% compared to the theoretical performance obtained by doubling the actuation displacement of the theoretical nestled behavior of the two individual rib knit pattern knit textiles (shown with a dashed teal line in Figure 34). The stacked-nested architectural configuration produces a maximum of 11.5 mm of displacement under a 39.0 N or 3.9 kPa, nearly doubling the displacement of the individuals (6.4 mm and 6.3 mm) under the additive loading at max displacement for the individual textiles (13.7 N or 1.4 kPa and 24.7 N or 2.5 kPa), meeting the displacement criteria for flow control applications. At the optimal operating point, the maximum work production point, the stacked-nestled rib knit pattern knit actuator produces 6.8 mm of displacement under a pressure of 15.4 kPa, realizing the load (10 to 16.5 kPa) and approaching the deflection (10 to 30 mms) requirements for distributed flow control devices. While both of these maximum performance points are just outside the application specification region, a large portion of the predicted pressure displacement curve between the max displacement and max work point meet the application specifications. By stacking a third nestled prototype on top of the current stacked-nestled configuration it is theoretically possible to reach the load and displacement simultaneously. It is predicted that three stacked two nestled prototypes would produce 18.8 mm of actuation motion under a 3.1 kPa applied load at the maximum displacement point (shown by the cross on the orange dashed line in Figure 34) and 11.1 mm of actuation motion under a 14.5 kPa applied load at the maximum work point (shown by the x on the orange dashed line). The three stacked-2 nestled architectural is predicted to produce the needed displacement at aerodynamic loads to provide local surface modification to provide flow control.

4.3. FEASIBILITY DEMONSTRATION STUDY CONCLUSIONS

This section investigated the potential of active knits to be used in an application requiring distributed surface actuation: contour bumps for flow control. Contour bumps have the potential to enhance flight efficiency by delaying separation of or by reattaching the boundary layer; however, no actuators currently exist to provide the desired actuation motion during flight. The goal of this section was to demonstrate the feasibility of active knits by identifying a potential application, defining the technical specifications for the application, choosing a knit architecture to meet the kinematic motion needs of the application, and experimentally testing active knit prototypes to meet the kinetic technical specifications.

The specific application, a contour bump for flow control over an airfoil, was chosen and the technical specifications (displacements on the order of 10-25 mm under aerodynamic level loads of 10-16 kPa) of the application were determined by analyzing existing literature on the theoretical study of transonic contour bumps. The rib knit pattern was chosen for the flow control feasibility demonstration study because it produces large surface displacements under significant applied loads by transforming from a nearly planar surface to a series of raised and lowered ridges. The rib knit pattern actuator could be used as an embedded surface actuator that

is placed beneath the skin of the wing and the actuation displacement can be used to create local shape modification by contouring the surface of the wing.

Individual, stacked, nestled, and stacked-nestled rib knit pattern prototypes were experimentally tested to determine their actuation performance capabilities compared to flow control specifications. Four individual rib knit pattern prototypes were created using a 2x2 rib knit pattern with 20 mil 70°C Flexinol® wire on 6.0 mm knitting needles for 14 loops and 16 rows. The four prototypes were experimentally tested, individually and in configurations, to obtain the actuation displacement in response to an applied constant load. Each of the individual prototypes and configurations displayed the same behavior as displayed by garter knit pattern active knit actuators discussed in section 3, as the applied load was increased the actuation displacement increased up to a maximum actuator displacement then further increased applied loads resulted in decreased actuation displacements. The individual prototypes provided nearly identical performance (average displacement error of 7.7%), producing maximum actuation displacements of 6.3 and 6.4 mm against loads of 2.5 and 1.4 kPa. The individual textiles were stacked on top of each other, creating the stacked prototype, and acted in series to double the actuation displacement to 12.6 mm under an applied pressure of 1.8 kPa. An additional architectural configuration, nestling, enhanced the operational pressure by allowing the textiles to work in parallel, producing 6.3 mm deflection under 4.8 kPa. A stacked-nestled prototype was shown to simultaneously improve the pressure (from 1.8 kPa to 3.9 kPa) and deflection (from 6.3 mm to 11.5 mm) over each the stacked and the nestled configurations. It is predicted that both the displacement and loading requirements for flow control applications can be met by stacking three sets of two nestled textiles on top of each other.

This feasibility demonstration study has shown that rib knit pattern active knits can meet the performance specifications required for flow control of an aircraft. The rib knit pattern, which expands out-of-plane, provides a new actuation motion that is unattainable with current technologies. The out-of-plane expansion produces very large actuation motions on the order of 100%, under large, application level loads. Additionally, an amplification scheme that improves kinetic performance was identified. The stacked and nestled architectural configurations enhanced the performance of the rib knit pattern through series and parallel connections of prototypes. Beyond the immediate results, this case study investigates an effective way to use the unique motions created by active knits and demonstrates the ability to create large actuation motions under application level loads. The series and parallel connections approach can be used to improve the kinetic performance of all knit architectures by identifying the manner in which the load is transferred and the motion is created. The approach of identifying an application that could be improved, identifying the motion required to achieve the application, choosing an active knitted architecture to produce the desired motion, and using amplification techniques such as series and parallel connections to meet the application specifications could be implemented for other applications. This case study has demonstrated the potential of the rib knit pattern to meet the technical specifications for this flow control application and shows that active knits are a promising technology to meet the kinetic and kinematic requirements of modern applications by producing simultaneous radical forces and displacements in the form of complex distributed motions in a small package.

5. OUTCOMES AND LEARNINGS

The Air Force has a growing need for super-configurable multifunctional structures that can alter their shape, functionality, or mechanical properties in response to operational conditions. One such application is morphing aircraft that can adjust their wing geometry to expand the aircrafts' operational platform and maneuver over a wide range of flight regimes. Flow control in the form of varying the topology of the wing to delay or reattach a separated boundary layer to reduce drag and improve flight efficiency is another application that promises improved performance. Additionally, deployable space systems are needed to compactly deliver payloads to the upper atmosphere to be deployed and reconfigured for surveillance operations. Active membranes are needed to realize applications such as flapping wing vehicles. All of these applications require active structures capable of radical shape changes distributed over a surface that can support aerodynamic loads while being light weight, compact, and robust. Active knits are a new cellular architectural paradigm with potential to revolutionize actuators by producing simultaneous radical forces and displacements, in the form of complex three-dimensional actuation motions distributed throughout a structure, all in a small package size.

5.1. RESEARCH RESULTS

The results of this research established the fundamental science basis for active knit architecture, a new enabling technology. Three major efforts were completed: 1) a classification of active knit architectures and their kinematic actuation motions, 2) an analytical predictive model of the active knitted loop actuation performance, and 3) a feasibility demonstration case study on an air flow control application.

5.1.1. Active Knit Hierarchical Architecture

The cellular structure of active knits enables a huge variety of possible architectures providing any number of varied actuation behaviors. To enable the effective use of the active knit technology in applications a formal language that describes the active knitted architecture was constructed. The hierarchical architecture classification structure allows the identification of the actuation mechanism and the determination of the impact of architecture on kinematic actuator performance. In order for the active knit hierarchy to reveal the breadth of kinematic actuation motions produced by active knits, the knitted hierarchy describes four component levels: knitted loop, knit pattern, grid pattern, and restructured grid, where each level relates to a different aspect of performance and behavior of the entire knitted textile. The knitted loop leverages bending in the smart material to create larger actuation motions. The knit pattern, a homogeneous arrangement of knit and purl loops in the knitting grid, transforms the individual motions of the knitted loops into distributed actuation behaviors. Grid patterns, heterogeneous patterns of knit and purl loops, produce different motions over different regions of the textile. Restructured grids, modified orthogonal knitting grids, transform and expand the type of motions produced at the lower levels of the hierarchy. This common language for discussion and complete understanding of the interactions between levels of the active knit hierarchy provides a basis for deriving models and aids in designing active knit architectures capable of producing desired complex, three dimensional motions specifically customized to a given application.

5.1.2. Two-Dimensional Analytical Model

The complex structure of an active knit requires a detailed model to relate stress-strain behavior of the underlying active material to the force and motion performance of the knitted textile. This research expanded upon existing knit models to capture the cyclic actuation behavior of planar active knits by incorporating the dual states of the material and the various friction states between interlacing adjacent loops. The active knit predictive model was developed defining the operational states, identifying and geometrically defining the smallest repetitive unit cell, developing predictive capabilities of the active knit loop and garter knit pattern active textiles, and experimentally validating the model. Outlining the multi-state actuation cycle was key to capturing the actuation behavior including the mechanical and thermal operational transitions the textile undergoes during deformation as well as the statehistory dependent friction interactions within the structure. Analytical modeling techniques were employed to produce a set of fully analytical transcendental algebraic equations (as opposed to a set of coupled differential equations) to describe the deflections experienced within a unit cell for each operational state. The analytical form allows the equations to be easily scaled to produce the load-extension properties of the entire knit pattern textile for each state as well as the net actuation performance, and provides a better understanding of the effects of each geometric and material design parameter. The fast computation of an analytical model relative to a finite element approach enables broad parameter studies from which extensive design guidelines can be constructed, and allows a designer to tailor the performance of an active knit architecture to meet specific application requirements.

5.1.3. Feasibility Demonstration

Active knits have a great potential for complex distributed motions, but it was still necessary to demonstrate that their radical forces and motions were sufficient for the demanding needs of Air Force applications. The chosen case study application, contour bumps for flow control, has the potential to enhance flight efficiency by delaying separation of or by reattaching the boundary layer, although no actuators currently exist to provide the desired actuation motion during flight. The rib knit pattern, which expands out-of-plane, provides a new actuation motion that is unattainable with current technologies. The out-of-plane expansion produces very large actuation motions on the order of 100%, under large, application level loads distributed over the surface in a very thin, compact package. The specific requirements for airfoil contour bumps were identified and it was experimentally demonstrated that the active rib architecture was capable of meeting the specifications when combined in a stacking and nestling architectural configuration to amplify both the forces and motions produced by the basic knit textile. This amplification scheme provides additional means to fit the performance of an active knit to the needs of a specific application and greatly extend the actuation capacity of this already powerful technology to the demanding actuation needs of the Air Force.

5.2. SIGNIFICANT LEARNINGS

These results provide a number of significant learnings which provide the Air Force with new capabilities which can be extended to a wide variety of application needs.

5.2.1. New Capabilities

The hierarchical architecture of active knits enables a wide array of actuation motions that are unattainable by conventional or traditional smart material actuators. The distributed

actuation provided by active knits allow for motions over entire surfaces and throughout a structure to be generated without the need for complex, heavy, and bulky mechanisms to distribute the motions produced by point actuation. The unique shapes of motions producible by active knits can enable applications through self-furling and unfurling deployable structures, surface texturing for flow control, radically morphing-wing aircraft, contour bumps and other surface reshaping, compact torque generation, and extreme contractile actuation. Such applications of active knits could allow aircraft to adapt to a range of flight regimes, reacting to changing mission parameters, and improving overall efficiency and range, as well enabling deployable space structures with adjustable geometry for adaptive antennas, solar panels, and optics.

5.2.2. Unprecedented Performance

Active knits exploit the performance of the underlying smart material in a way that can extend the performance well beyond that of the original material. In particular, the extremely high energy density of shape memory alloy is leveraged through the knit architecture to produce extreme strains (on the order of 70% in contraction, over 100% in expansion, and as much as 400% in deployment) while working against significant forces (upwards of 7N and equivalent pressures of 12kPa). In addition, the performance can be scaled through combinatorial architectures to produce forces and displacement several times larger than the knit textile. These levels of simultaneous force and motion are produce from an extremely lightweight and compact package and are out of the range of other existing technologies. Such extreme performance can enable actuation in aircraft across a variety of scales from small UAV to full size aircraft providing more actuation in a smaller space than otherwise possible, lowering the weight, improving the maneuverability and efficiency of aircraft, as well as allowing for longer ranges with larger payloads.

5.2.3. Varied, Customizable Behavior

In addition to the extreme performance afforded by active knits, the hierarchical architecture enables a boundless variety of different motions. The understanding of the interactions between the hierarchical levels developed in this work provides the means to design and customize any desired behavior through the appropriate distribution of unit cell types, knit patterns, grid patterns, and grid restructurings. The existing catalog of available behaviors is only a first guide to the possible motions which can be produced by active knits. The demonstrated behaviors can be combined or modified and new behaviors can be created to suit any actuation need. This work provides the building blocks and framework by which these behaviors can be constructed, limited only by the imagination of the designer. Any number of functionalities could be incorporated into aircraft in this manner including large motion control surfaces providing extreme maneuvering in UAV's, adaptive radar profile for improved stealth, and multi-mode flight for enhanced and adaptive mission flexibility.

5.2.4. Predictable, Tailorable Performance

The experimentally validated analytical performance model provides not only the means to predict the performance of an active knit, but also enables the performance of the knits to be tailored to meet given actuation requirements. The models expose the effects of individual design parameters from which designs can be developed. This ability to relate design choices to actuator performance is critical for producing performance tailored actuators which can be

fabricated through changes in design parameters such as wire diameter, loop size, as well as architectural parameters such as knit pattern repetition. Predictable, tailorable performance allows actuators to be produced with the best possible performance, and performance specifically suited for an application. Highly tailored actuation would enable functionality with a minimum use of power, weight, and space, lowering drag, decreasing fuel use, and increasing the range and flexibility of aircraft.

5.2.5. Extensible Modeling Methodology

The model developed in this work was specific to a particular planar knit architecture, but the methodology followed is directly extensible to other active knit architectures as well as to passive knit applications such as in composite materials. The methodology supports the inclusion of additional effects such as stick-slip friction, distributed thermal environment, three-dimensional motions, and distributed external contact. Thus, predictive models of new configurations can be built upon the fundamental framework developed here providing the ability to design and tailor the performance of a wide variety of architectures and applications. This would allow aircraft using active knit actuators to be designed to operate precisely in a wide range of environments from high altitude to high temperature, and provide as much of the range-increasing and fuel saving benefits that active knits promise, even in the most complex situations.

5.2.6. Extendable Domains

Shape memory alloy was selected as the primary material for this study, but the active knit architecture applies to any active material fiber. Shape memory alloys excel at producing large forces and motions from thermal activation, but other materials have other advantages. For example, piezoelectric materials produce less strain, but can operate at ultrasonic frequencies. An active knit constructed of piezo fibers can leverage the motions into moderate-stroke high frequency electrically activated actuators which can enable an even wider array of applications. By selecting an appropriate active material fiber, active knit textiles can be produced to operate within a huge variety of frequency, environmental, stroke, and activation domains, providing an enabling technology for a multitude of Air Force applications. Thus, applications such as UAV's and MAV's with high speed flapping wings or with extremely quick, agile maneuverability can be enabled by active knit architectures.

5.3. FUTURE DIRECTIONS

This research forms the foundation for active knit architectures but there is still work to be done to make this new technology available to Air Force applications.

5.3.1. Three-dimensional Modeling

The modeling work reported here has focused on two-dimensional knit architectures. To apply the benefits of predictable, tailorable performance to the wide variety of available architectures with complex motions, this model must be extended to three dimensions. A three-dimensional analytical model can be developed by extending the modeling techniques used for the two-dimensional model. Ideally, a model would be created using a three dimensional unit cell with boundary conditions that could be manipulated to form any knit or grid pattern imaginable. However, even the simplest knit pattern (stockinette) requires capturing large three-dimensional rotations while more complicated knit patterns (such as rib) also require the implementation of an extended unit cell as adjacent loops are asymmetric due to the alternating

pattern of the knit and purl loops in the knit pattern. Extending the modeling techniques and producing three-dimensional knit architecture models broadens the scientific basis enabling a wider array of applications.

5.3.2. Experimental Methodologies

A model must be experimentally validated to ensure the accuracy of its predictive capabilities. Because each of the active knit architectures display radically different kinematic actuation behaviors a different experimental setup and procedure is needed for each knit architecture. When designing the experiments it is necessary to ensure that each active knit architecture is tested for a particular motion and loading profile that is related to a potential application because a single type of experiment cannot capture and characterize the behavior of all active knits. In addition to custom designed experimental setups and procedures, new experimental techniques are needed to track the shape of individual loops within the textile during actuation. New experimental setups, procedures, and techniques are needed to validate the active knits models and identify any limitations to the model including sensitivity to different design parameters.

5.3.3. Design Guidelines

Design guidelines are needed to improve usability of the active knit actuation architecture. Parameter studies should be conducted and the models should be exercised to develop design guidelines that govern kinematic and kinetic behavior. Parameter studies need to be designed to identify the importance of each of the geometric design parameters –wire diameter, loop size, number of courses and wales – and their impact on kinetic performance. Additionally, it is necessary to establish strategies for the creation of architectures that provide a desired kinematic motion. Design guidelines are essential to enabling others to design active knitted actuators with the appropriate architectural, geometric, and material parameters to meet application needs.

5.3.4. In-Situ Activation

One critical issue that must be resolved for future Air Force applications is the enabling of simplified electrical activation and control. Active knits are produced with a continuous strand of an active fiber that creates interlocking adjacent loops. The interconnectivity of the knitted architecture prevents electrical activation due to shorting across the structure. One potential solution to this problem is to coat the active fiber with an electrically isolating coating. While coated shape memory alloy fibers are under development and just becoming available, which may solve the electrical connectivity issue, it is unknown how the coated fibers will perform both within and outside the knitted architecture. The fiber coating may affect the mechanical behavior of the SMA wire as well as the heating and cooling timing and required input power. It also may impact the friction behavior between interlacing adjacent loops. In addition to affecting the kinetic actuation performance of the active knit the coating may provide material degradation including wear, fatigue, debonding, and reduced environmental robustness. Understanding the effects of wire coatings on the performance of active knits is critical for advancing the technology to where it can be used in Air Force applications.

5.3.5. Active Knit Composites

Many applications would benefit from an active knit embedded in a flat-sheet compliant matrix rather than a bare knit textile to provide functionality such as an aerodynamically smooth surface, environmental isolation, or even a self-contained return spring to re-stretch the knit when it is deactivated. Several key research issues exist to enable this including 1) selecting the proper material such as a silicone rubber or polyamide which can adhere to the knit fibers and provide enough compliance to accommodate the large strains produced by the knit, 2) developing coating techniques which allow relative slip between adjacent loops, 3) thermal activation through the matrix, and 4) predictive models of active knit composites to enable predictable, tailorable performance. With these issues addressed, a new array of applications can be enabled.

5.3.6. Application Development

Finally, with all the tools for the design and use of active knits in place, a case study application can be identified and developed. Ideally, this would be an Air Force application which requires the unique capabilities of active knits and provides a critical and new functionality to the Air Force. Such an application would demonstrate the new enabling capabilities provided by active knits and validate the design guidelines and methodologies developed throughout the work. In performing the case study, additional practical issues may arise such as attachment to structure, vibration sensitivity, lifetime, etc. which need further study to address. Candidates for such a case study include compliant control surfaces for UAV's, adjustable textured surfaces for flow control, and adjustable wing shape for variable flight regimes.

5.4. POTENTIAL IMPACT

Active knits have the potential to meet the demand for advanced actuators as enabler for new and higher performance aircraft. The radical forces and strains and complex, distributed, three-dimensional behaviors of these architectures go well beyond anything currently accessible through traditional actuation or conventional smart material actuation architectures. This novel technology will make possible advancements in current applications (shape morphing, flow control, deployable structures, safety mechanisms, medical devices, etc.), as well as open the door to applications yet conceived, enabling lighter weight, longer range aircraft with greater maneuverability and fuel efficiency, extended flight regimes, and greater mission adaptability and flexibility.

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